



Detailed presentation of test cases

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Coupled TH model, Cast3M code: ... where we want to end up

– Heat transfer

$$\begin{pmatrix} \rho_w S_w C_w \epsilon + \rho_i S_i C_i \epsilon + (1 - \epsilon) \rho_s C_s + \epsilon \rho_i L \frac{\partial S_i}{\partial T} \end{pmatrix} \frac{\partial T}{\partial t} \\ = \nabla (\lambda_t \nabla T) + \nabla [\rho_w c_w T \cdot \vec{\nabla} p + \rho_w c_w T \cdot \vec{\nabla} z]$$

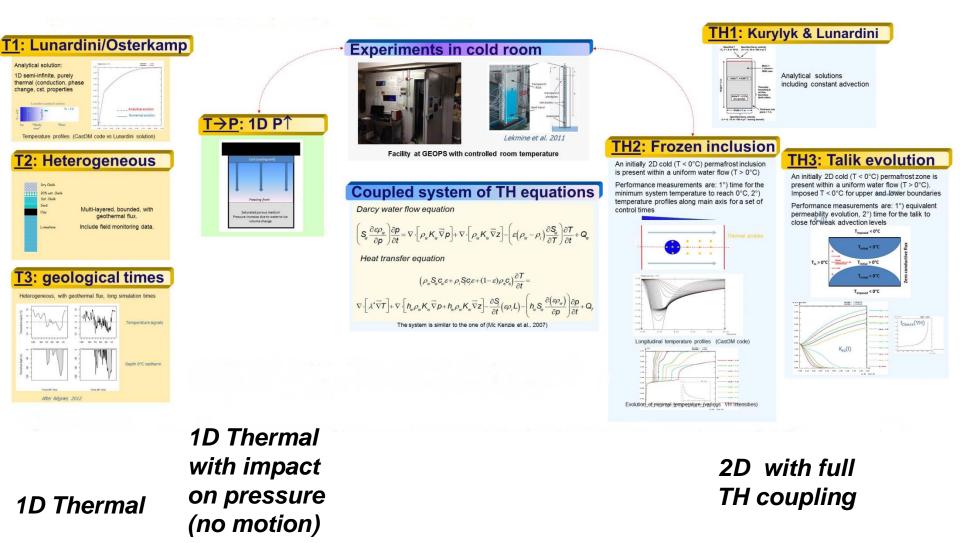
– Water transfer

$$\left(S_{w}\frac{\partial\epsilon\rho_{w}}{\partial\rho}\right)\frac{\partial p}{\partial t} = \nabla\left[\rho_{w}K_{w}\vec{\nabla}p\right] + \nabla\left[\rho_{w}K_{w}\vec{\nabla}z\right] - \left(\epsilon(\rho_{w}-\rho_{i})\frac{\partial S_{w}}{\partial T}\right)\frac{\partial T}{\partial t}$$

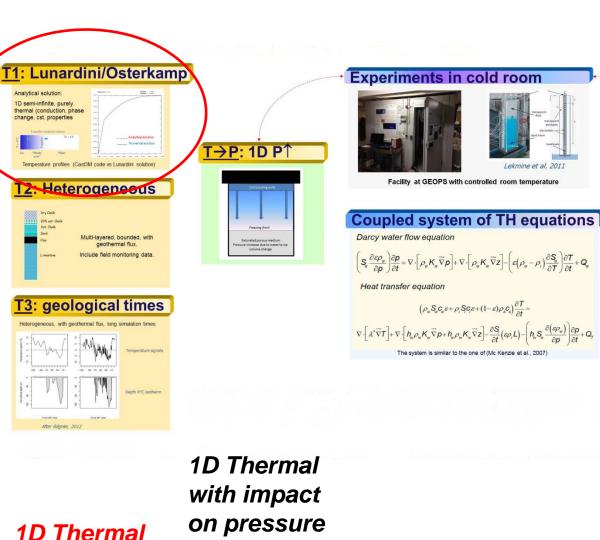
Program: from simple to complex !

- ➤ T1 T3: purely thermal, 1D
- T->P: pressure increases with freezing
- > TH1: advective term
- ➤ TH2, TH3: coupled cases

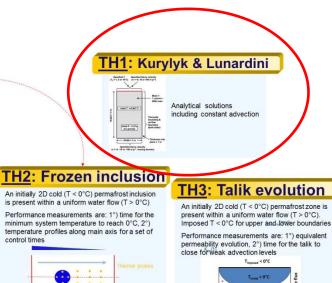
1D Thermal with advective component



1D Thermal with advective component



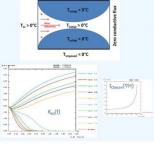
(no motion)



control times

Longitudinal temperature profiles (Cast3M code)

Evolution of minimal temperature (various VH Intensities)

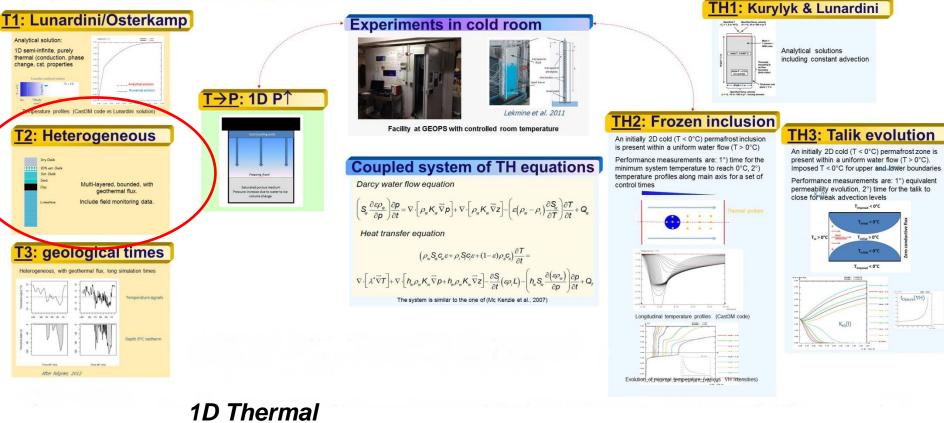


2D with full TH coupling

Analytical solutions: T1 and TH1

• B. Kurylyk & J. McKenzie

1D Thermal with advective component



1D Thermal

1D Thermal with impact on pressure (no motion)

2D with full TH coupling

Pure T: T2 and T3

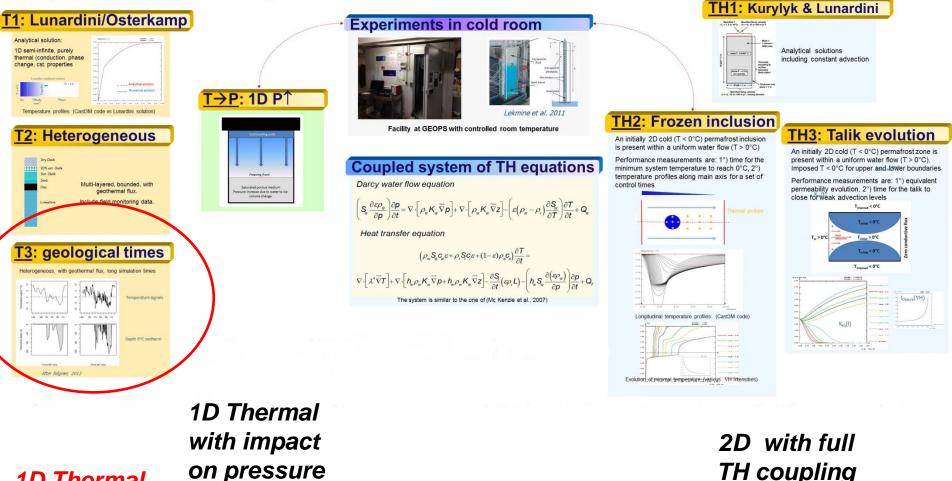
Bounded system, heterogeneity, geothermal flux

– Heat transfer

$$\begin{pmatrix} \rho_w S_w C_w \epsilon + \rho_i S_i C_i \epsilon + (1 - \epsilon) \rho_s C_s + \epsilon \rho_i L \frac{\partial S_i}{\partial T} \end{pmatrix} \frac{\partial T}{\partial t} \\ = \nabla (\lambda_t \nabla T) + \nabla [\rho_w c_w T \cdot \vec{\nabla} p + \rho_w c_w T \cdot \vec{\nabla} z]$$

T2 in discussion with climate modeling community

1D Thermal with advective component

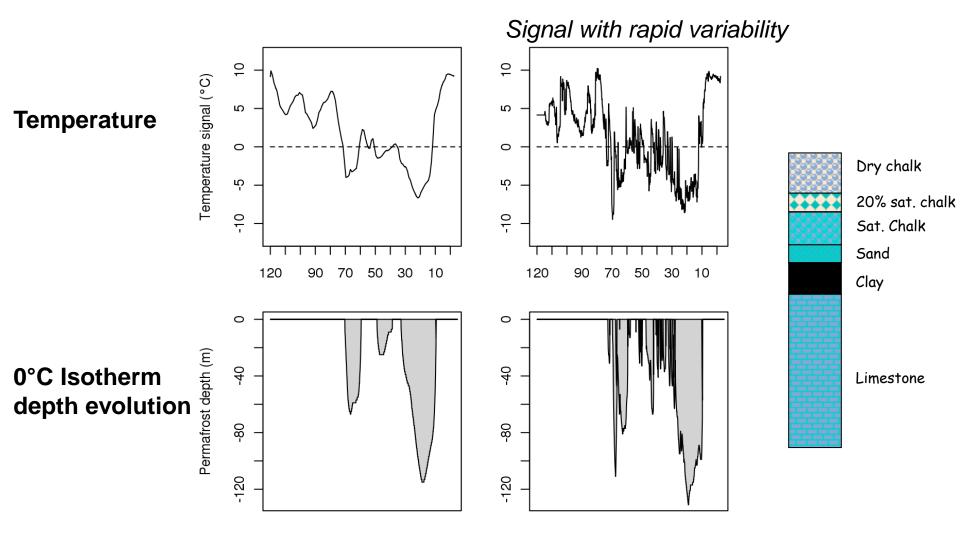


1D Thermal

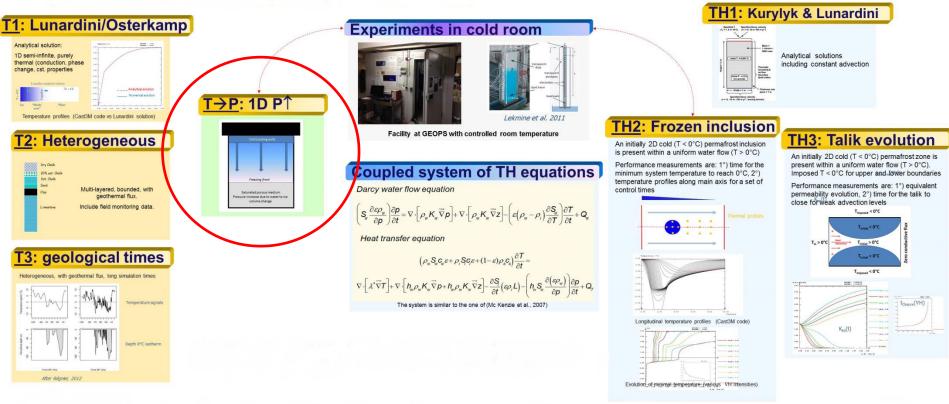
(no motion)

TH coupling

T3: long time evolution of permafrost depth



1D Thermal with advective component



2D with full TH coupling

1D Thermal with impact on pressure (no motion)

1D Thermal

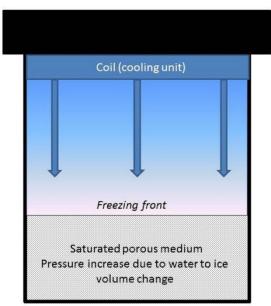


InterFrost Test Case T->P

$$\left(\rho_{w}S_{w}C_{w}\epsilon + \rho_{i}S_{i}C_{i}\epsilon + (1-\epsilon)\rho_{s}C_{s} + \epsilon\rho_{i}L\frac{\partial S_{i}}{\partial T} \right) \frac{\partial T}{\partial t} = \nabla . \left(\lambda_{t}\nabla T \right) + \nabla . \left[\rho_{w}c_{w}T.\vec{\nabla}p + \rho_{w}c_{w}T.\vec{\nabla}z \right]$$
$$\left(S_{w}\frac{\partial\epsilon\rho_{w}}{\partial\rho} \right) \frac{\partial p}{\partial t} = \nabla . \left[\rho_{w}K_{w}\vec{\nabla}p \right] + \nabla . \left[\rho_{w}K_{w}\vec{\nabla}z \right] - \left(\epsilon(\rho_{w} - \rho_{i})\frac{\partial S_{w}}{\partial T} \right) \frac{\partial T}{\partial t}$$

Pressure increase due to water freezing.

No fluid movement, constant volume (intended for code validation, not real world)

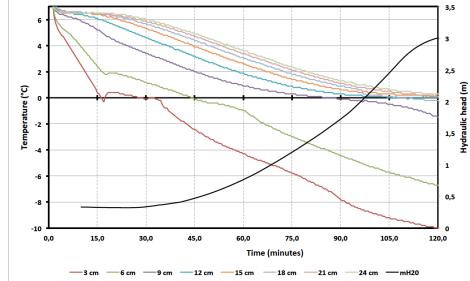


Monitoring of temperature (vertical profile) and water pressure in the unfrozen porous media

GEOSCIENCES

PARIS SUD

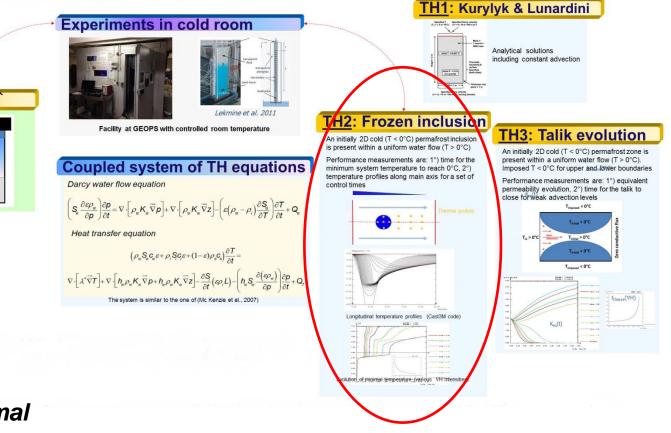
GEOPS



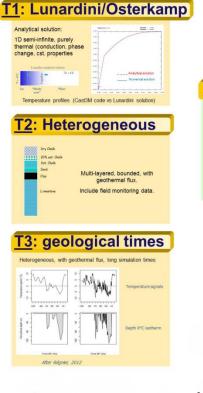
« controlled conditions »?

Side losses (minimized by insulation & cold room conditions) Total volume constant? (upper surface topography monitoring)

1D Thermal with advective component



2D with full TH coupling



1D Thermal





1D Thermal with impact on pressure (no motion)

Coupled TH model, TH2: Frozen Inclusion

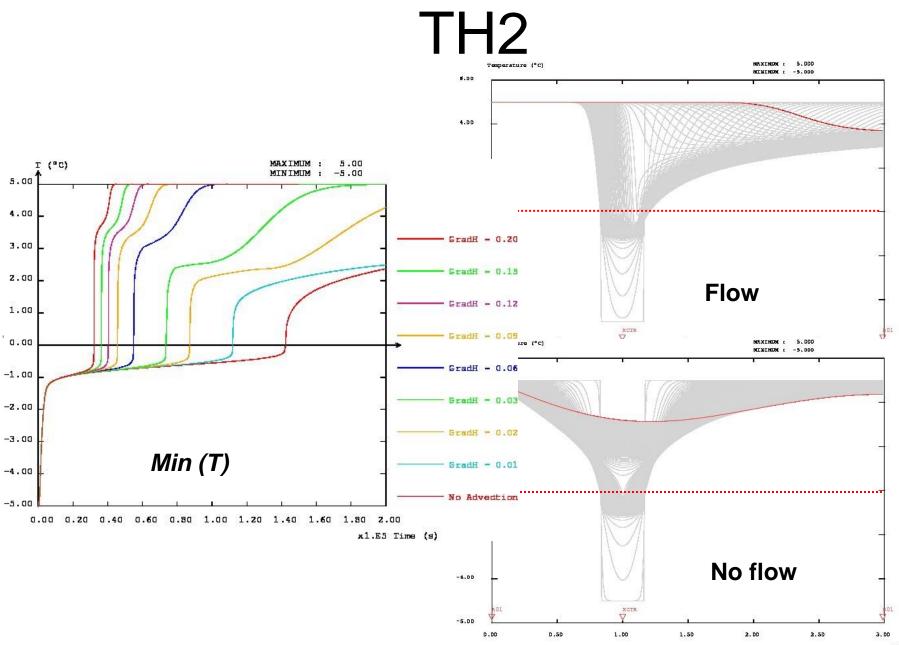
Sensitivity to water flow rates

 Heat transfer

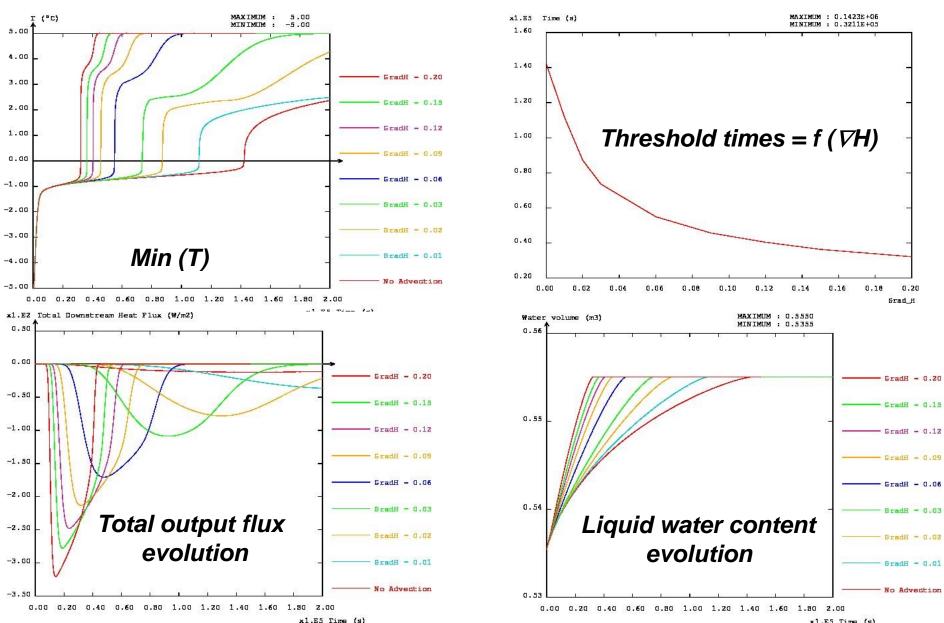
$$\begin{pmatrix} \rho_w S_w C_w \epsilon + \rho_i S_i C_i \epsilon + (1 - \epsilon) \rho_s C_s + \epsilon \rho_i L \frac{\partial S_i}{\partial T} \end{pmatrix} \frac{\partial T}{\partial t} \\ = \nabla \cdot (\lambda_t \nabla T) + \nabla \cdot \left[\rho_w c_w T \cdot \vec{\nabla} p + \rho_w c_w T \cdot \vec{\nabla} z \right]$$

– Water transfer

$$\left(S_{w}\frac{\partial\epsilon\rho_{w}}{\partial\rho}\right)\frac{\partial p}{\partial t} = \nabla\left[\rho_{w}K_{w}\vec{\nabla}p\right] + \nabla\left[\rho_{w}K_{w}\vec{\nabla}z\right] - \left(\epsilon(\rho_{w}-\rho_{i})\frac{\partial S_{w}}{\partial T}\right)\frac{\partial T}{\partial t}$$



TH2, performance measures

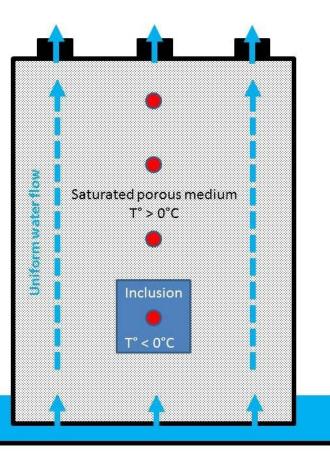




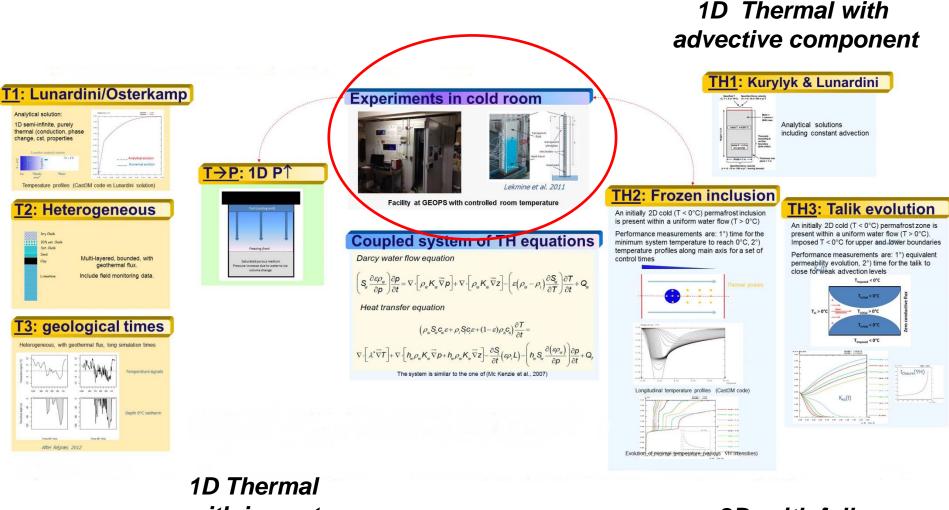


Lab. Experiment TH2 « Frozen Inclusion »

Monitoring of temperature (in the inclusion & downstream) Monitoring of water flow rate Measurement of transport velocity with tracer tests



*« controlled conditions »?*Side heat losses (minimized with insulation & cold room conditions)
Initial conditions *«* smooth *»*Control homogeneity of the porous medium (saturation & porosity)



1D Thermal

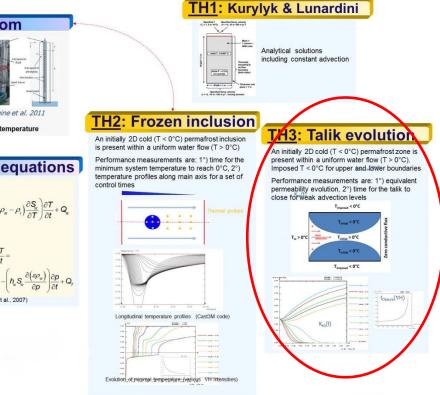
1D Thermal with impact on pressure (no motion)

2D with full TH coupling

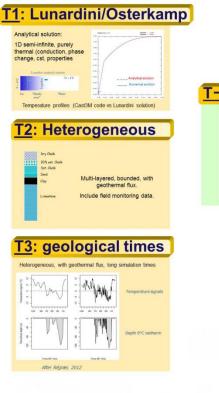
Experiments

- in cold room at GEOPS (Univ. Orsay)
- Visit tomorrow, chance to see them
- Still in a preliminary state

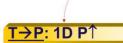
1D Thermal with advective component



2D with full TH coupling

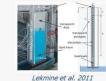


1D Thermal









Facility at GEOPS with controlled room temperature

Coupled system of TH equations Darcy water flow equation

 $\left(S_{w}\frac{\partial \varepsilon \rho_{w}}{\partial \mathbf{p}}\right)\frac{\partial \mathbf{p}}{\partial t} = \nabla \cdot \left[\rho_{w}K_{w}\vec{\nabla}\mathbf{p}\right] + \nabla \cdot \left[\rho_{w}K_{w}\vec{\nabla}\mathbf{z}\right] - \left(\varepsilon\left(\rho_{w}-\rho_{i}\right)\frac{\partial S_{w}}{\partial T}\right)\frac{\partial T}{\partial t} + Q_{w}$

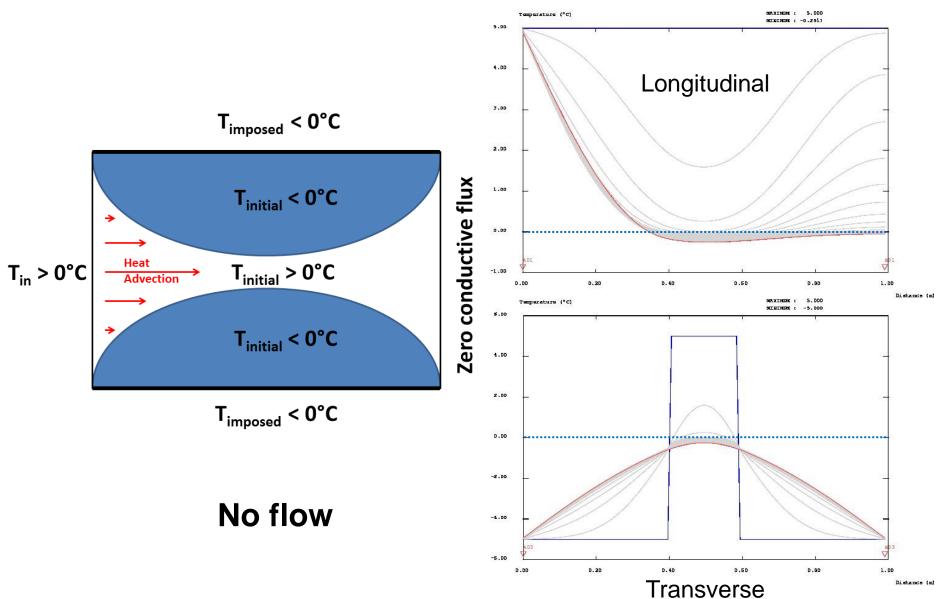
Heat transfer equation

$$\begin{split} & \left(\rho_{w}S_{w}G_{w}\varepsilon + \rho_{i}Sq\varepsilon + (1-\varepsilon)\rho_{s}G_{s}\right)\frac{\partial T}{\partial t} = \\ \nabla \cdot \left[\lambda^{*}\overrightarrow{\nabla T}\right] + \nabla \cdot \left[h_{w}\rho_{w}K_{w}\overrightarrow{\nabla}\rho + h_{w}\rho_{w}K_{w}\overrightarrow{\nabla}z\right] - \frac{\partial S_{i}}{\partial t}(\varepsilon\rho,L) - \left(h_{w}S_{w}\frac{\partial(\varepsilon\rho_{w})}{\partial\rho}\right)\frac{\partial\rho}{\partial t} + Q_{r} \end{split}$$
The system is similar to the one of (Mc Kenzie et al., 2007)

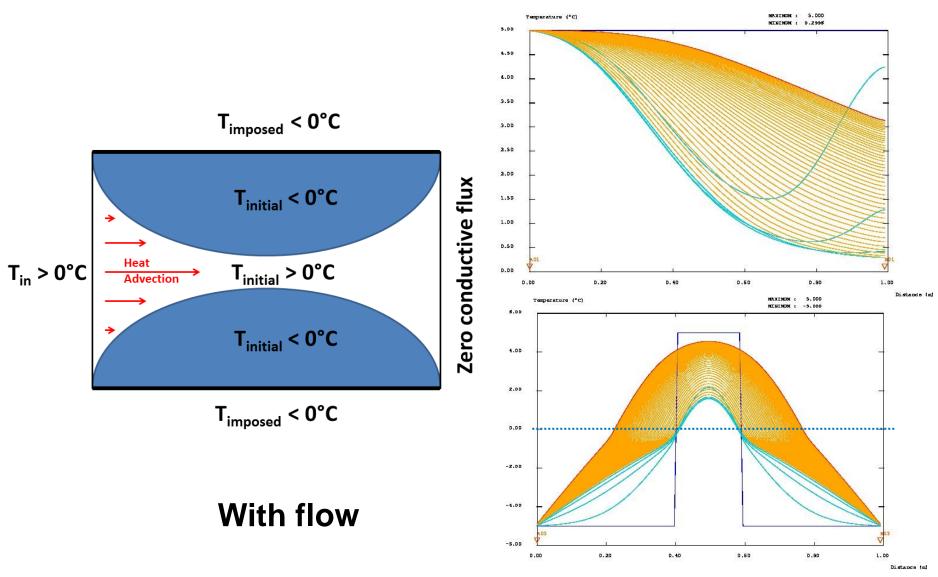
1D Thermal with impact on pressure

(no motion)

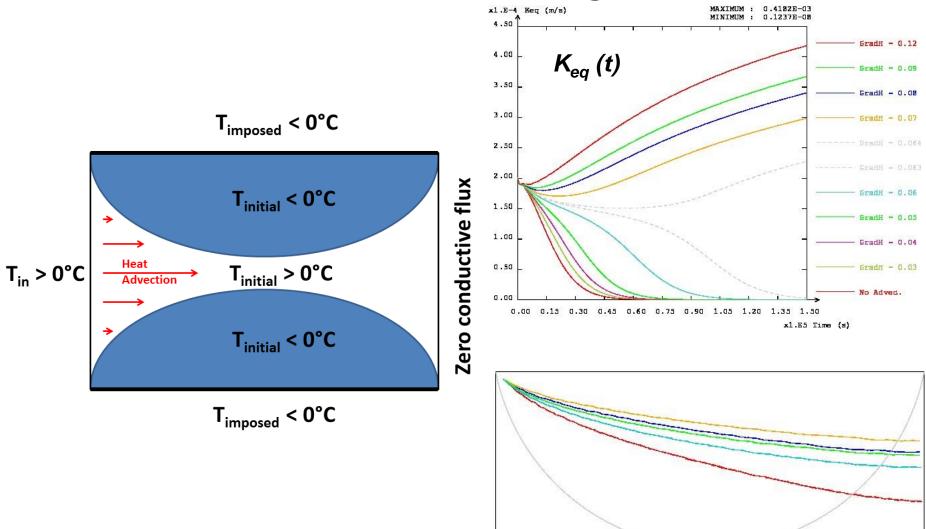
TH3: talik opening/closure



TH3: talik opening/closure

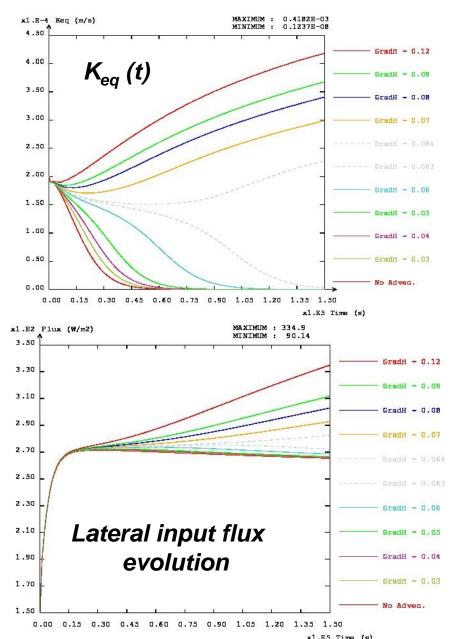


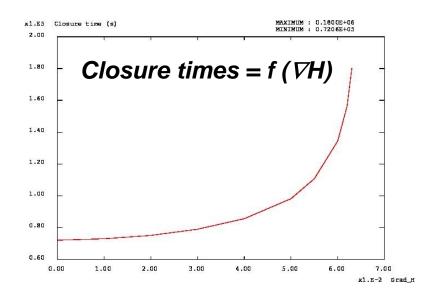
TH3: talik opening/closure

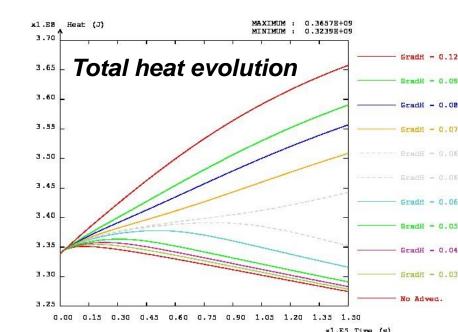


Steady state 0°C isotherm for opened tali

TH3, performance measures



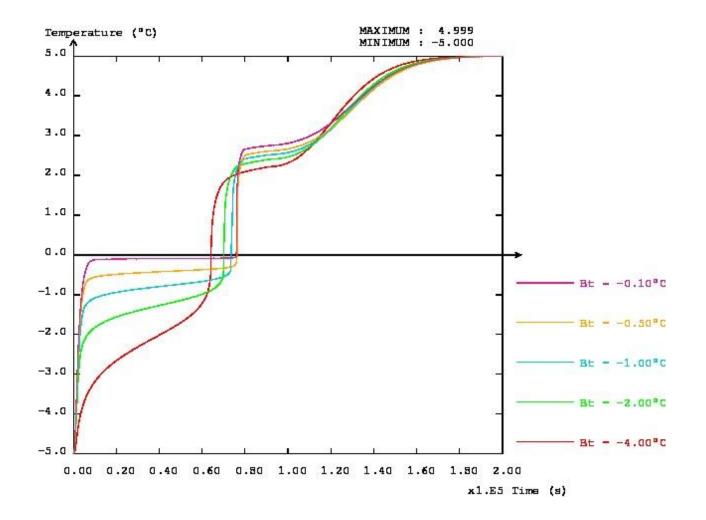




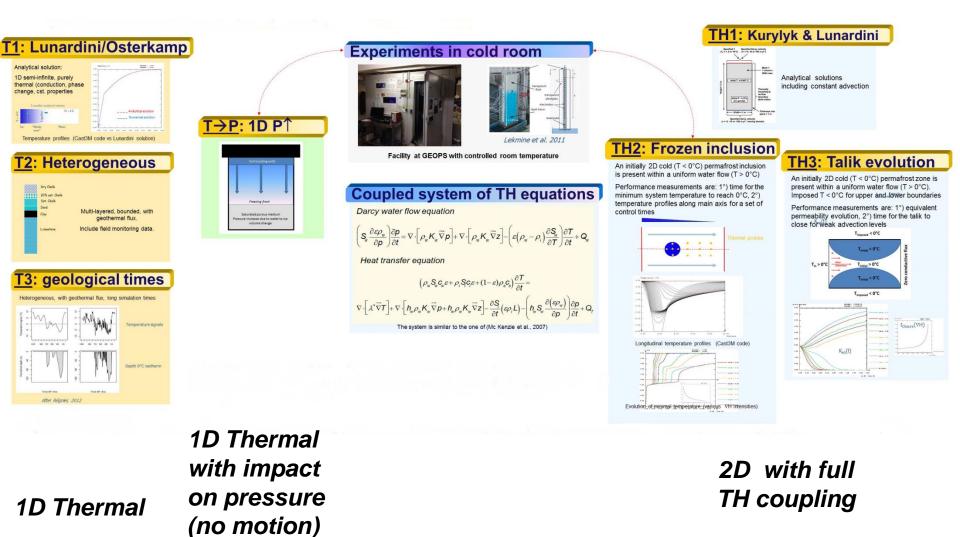
Convergence studies on TH2&3

- Simulations are converged
- What is the range of variation for the performance measures vor various discretisation strategies (spatial and temporal)? few percents
- Strong sensitivity to the liquid water saturation interval in the saturation curve!

Sensitivity to liquid water saturation interval for TH2

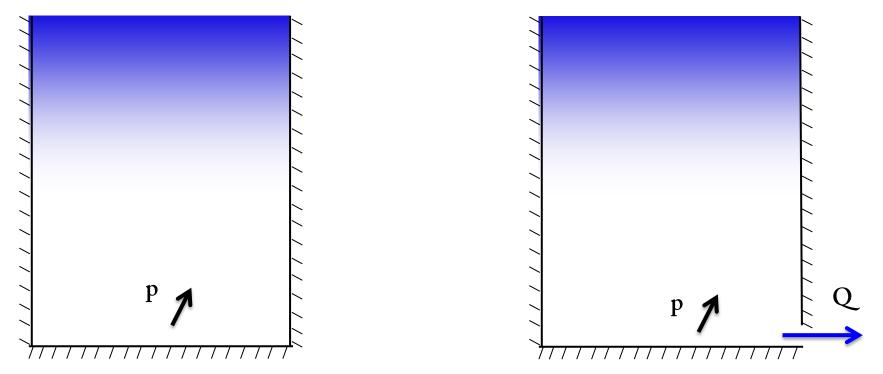


1D Thermal with advective component



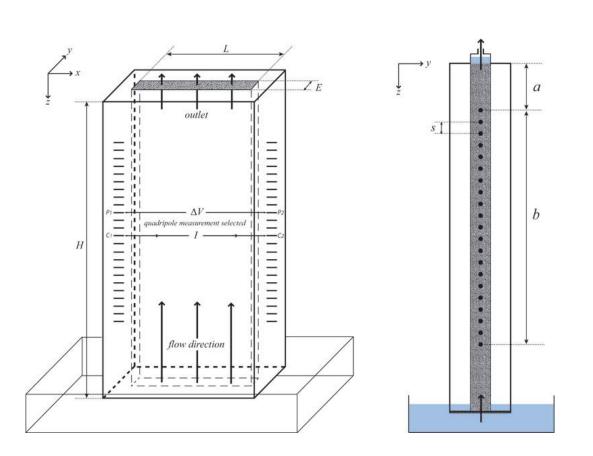
Pressure increase in confined layer (Task 2)

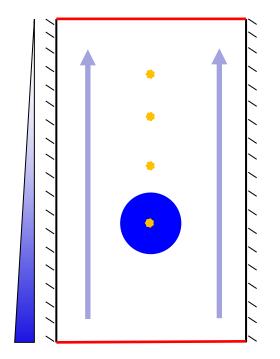
T < 0°C



T < 0°C

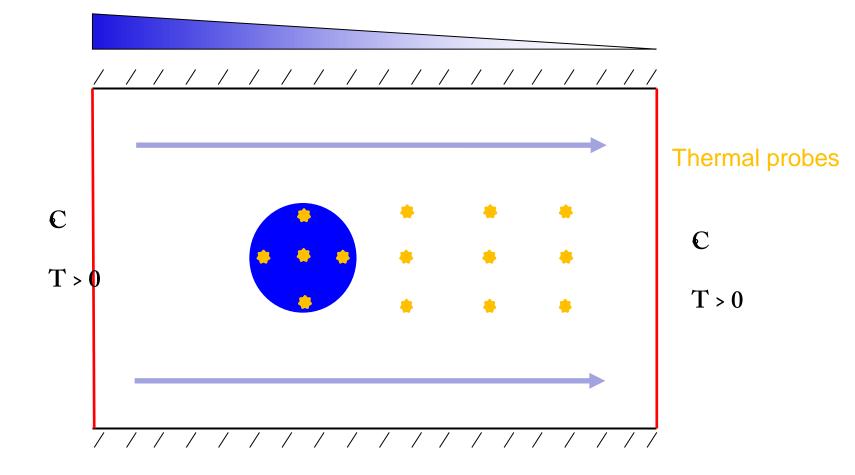
Associated cold room experiment at IDES, Paris Sud



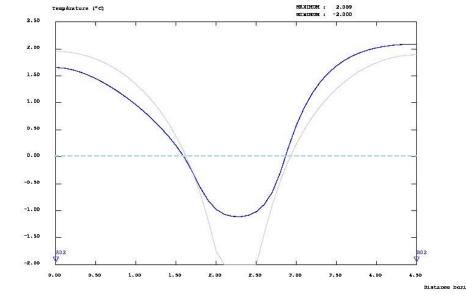


Lekmine et al 2011

Task 3: « uniform » water flow



Ice bubble or frozen water inclusion

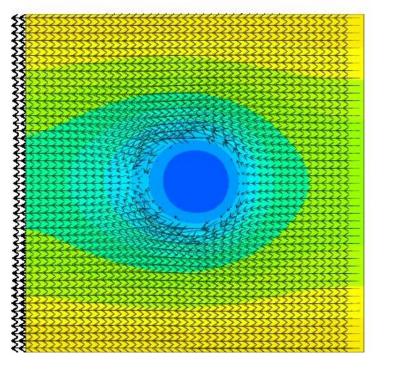


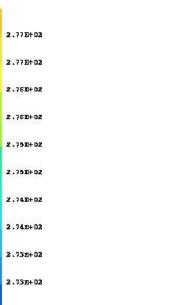
Températures à t = D ans, 5.D jours (59It; ErBest = 7.3E-5)

VAL - IBO

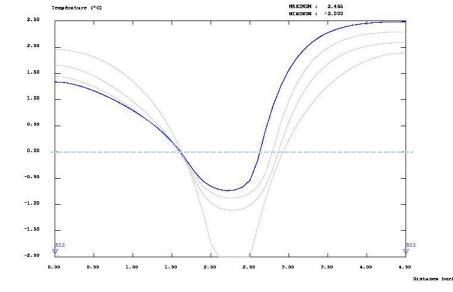
> Z.72E+DZ

< Z.77E+DZ



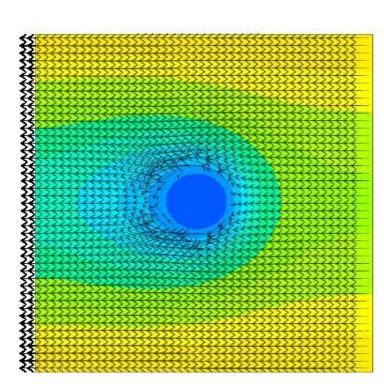


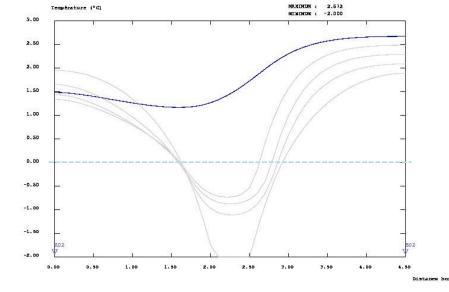
2.72E+D2



Températures à t = D ans, 15.D jours (20DIt; ErBest = 1.2E-3)

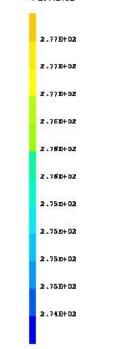
- VAL ISO > 2.72E+D2 < 2.77E+D2
- 2.772+02
- 2.77E+D2
- 2.75E+02
-
- 2.7510+02
- 2.75E+D2
- 2.75E+DZ
- 2.74E+02
- 2.74E+DZ
- 2.75E+02
- 2.75E+02
-
- 2.72E+D2

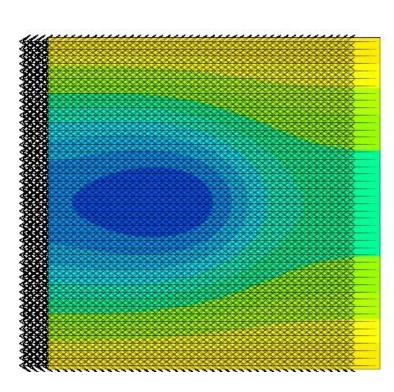


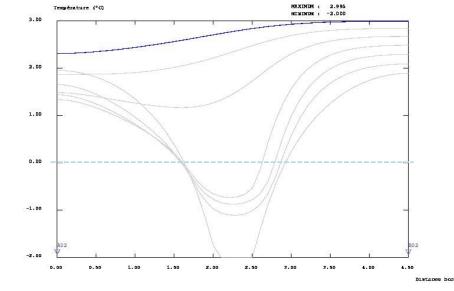


Températures à t = D ans, 20.0 jours (200It; ErBest = 7.1E-4)

VAL - IBO > 2.74E+D2 < 2.77E+D2







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Températures à t = D ans, 3D.D jours (3DIt; ErBest = 0.0E-5)
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- VAL IEO > 2.75E+D2 < 2.77E+D2
 - 2 . . 77 E+ D2 2 . . 78 E+ D2 2 . . 75 E+ D2

