

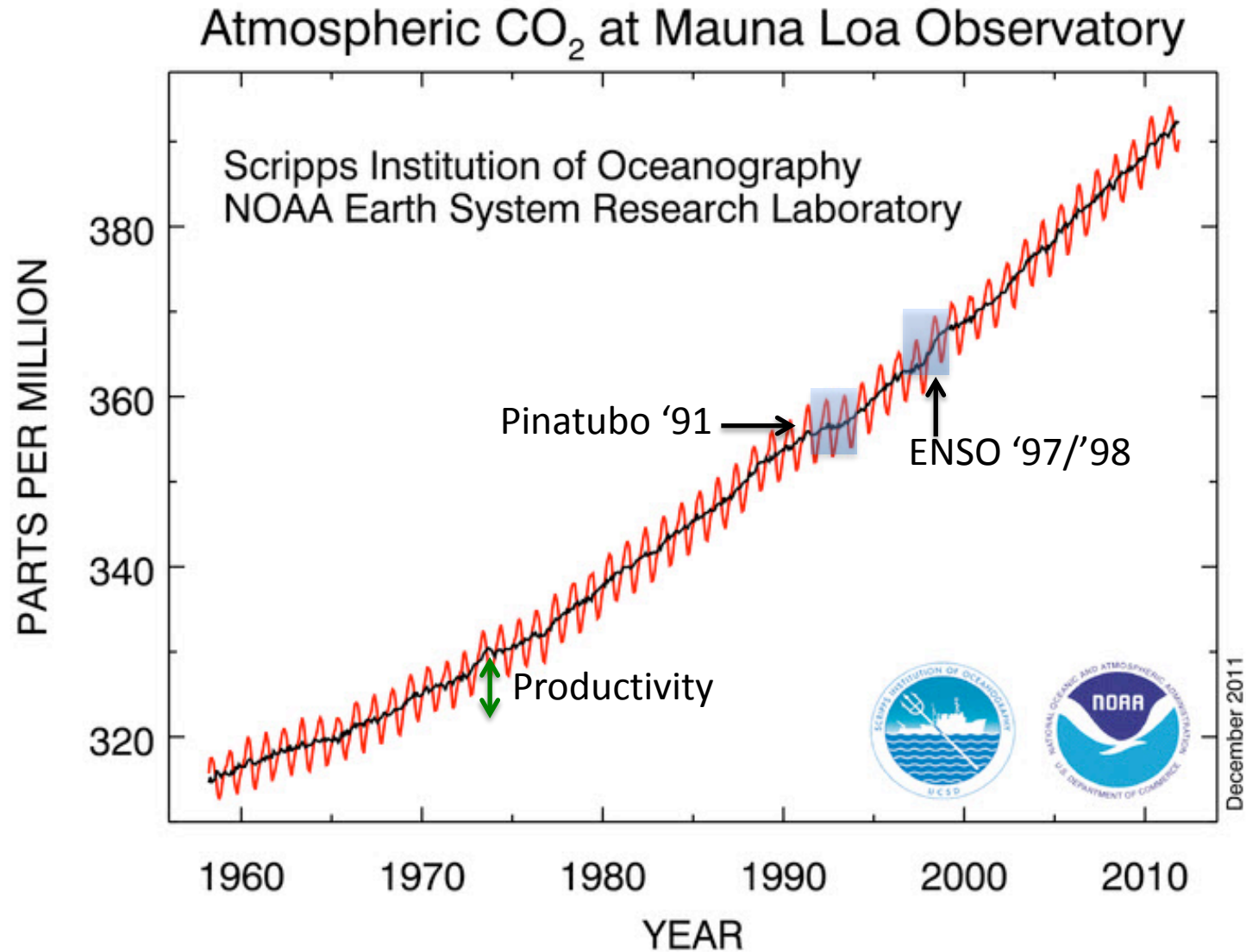
## Coupling carbon and water cycles in global vegetation models

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# Carbon and water cycling



## Goal of lecture

- Conceptual
  - Canopy processes
  - Photosynthesis
  - Conductance
- Technical
  - Approaches for modeling photosynthesis
  - Coupling photosynthesis and conductance



## Some variables

- $A$  ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ ): gross photosynthesis
- $A_{\text{net}}$  ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ ): photosynthesis –  $R_d$
- $R_d$  ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ ): leaf respiration
- $g_s$  ( $\text{mol m}^{-2} \text{s}^{-1}$ ): stomatal conductance
- $g_c$  ( $\text{mol m}^{-2} \text{s}^{-1}$ ): canopy conductance
- VPD (kPa): vapor pressure deficit
- RH (%): relative humidity
- $C_i$  (ppm): leaf internal  $\text{CO}_2$  concentration
- $C_a$  (ppm): atmospheric  $\text{CO}_2$  concentration



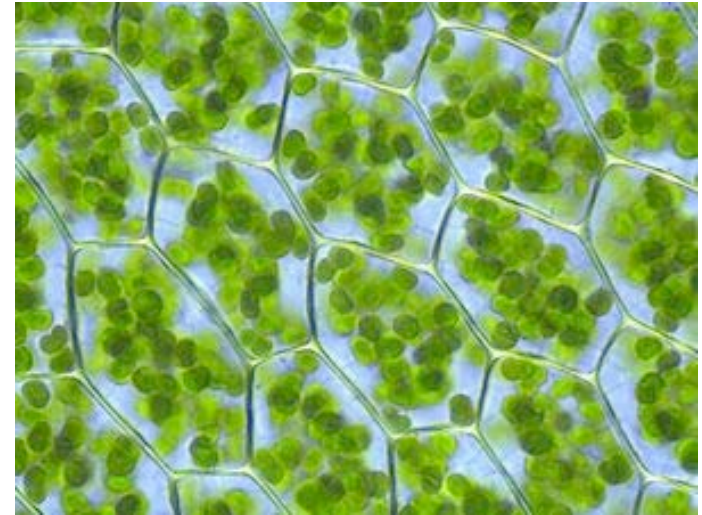
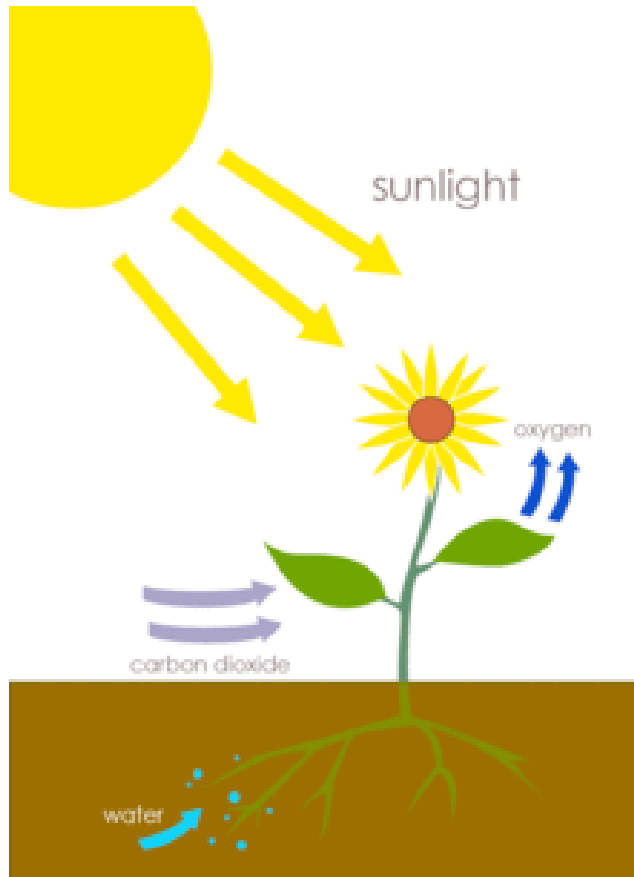
## Photosynthesis

- Conversion of  $\text{CO}_2$  to organic compounds (mainly sugars) using energy from sunlight
- 3.5 billion year old process
- Conducted by plants, algae, bacteria
- Oxygen ( $\text{O}_2$ ) is a waste product
- Globally, captures 100 Terawatts
- Global NPP 100-115 PgC



# Carbon and water cycling

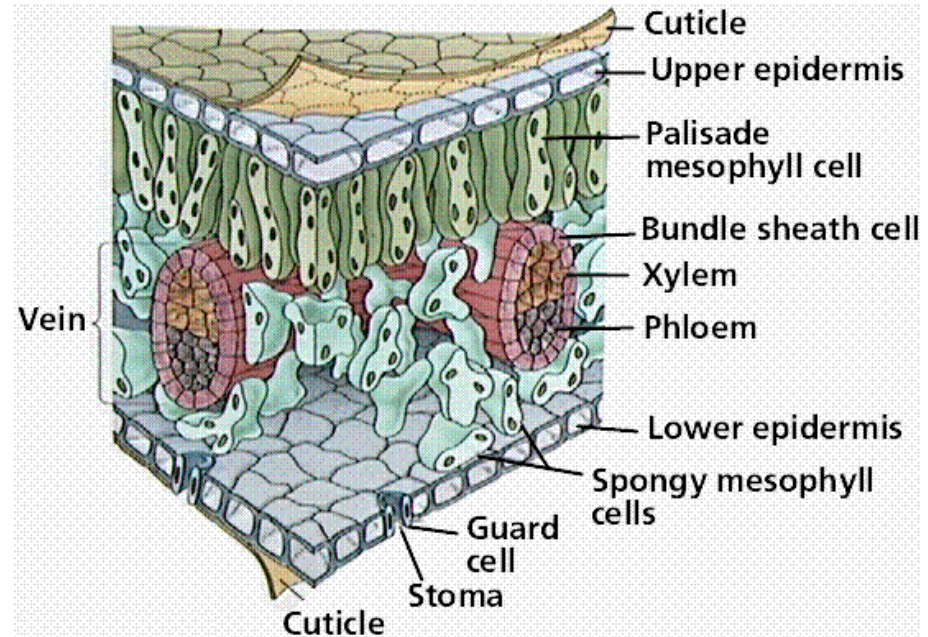
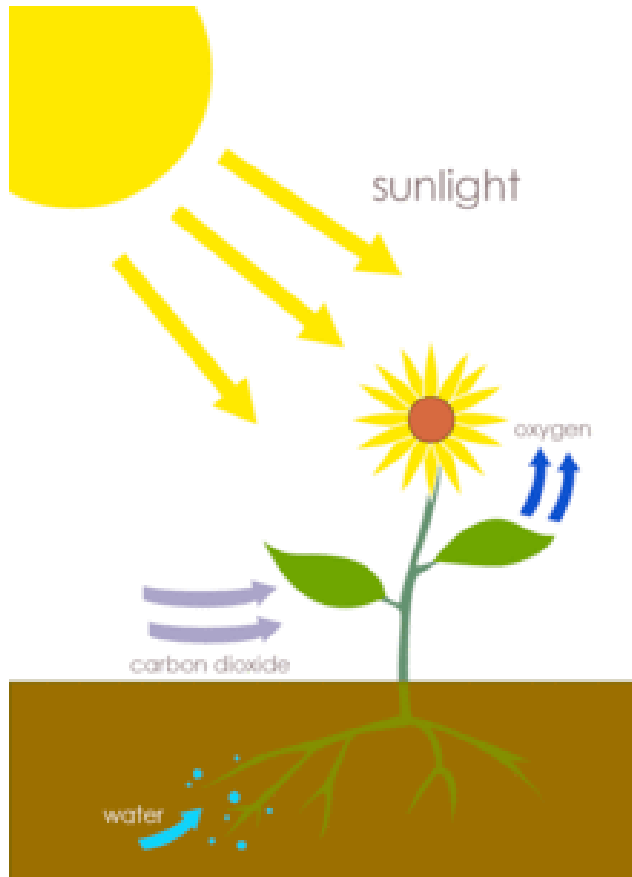
## Photosynthesis





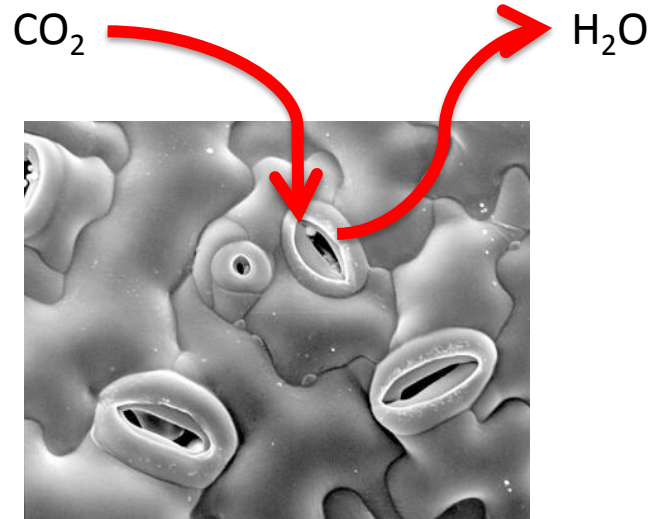
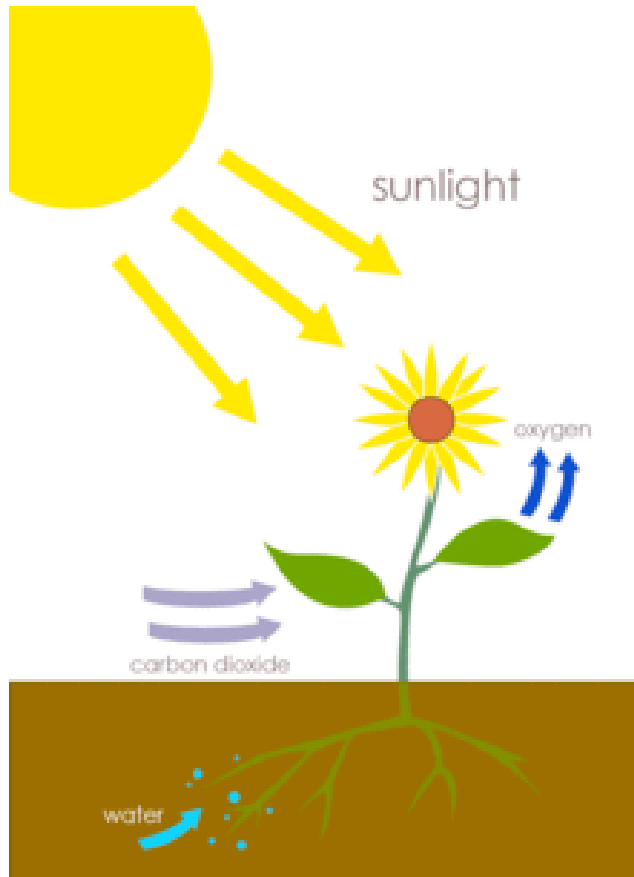
# Carbon and water cycling

## Photosynthesis



# Carbon and water cycling

## Photosynthesis

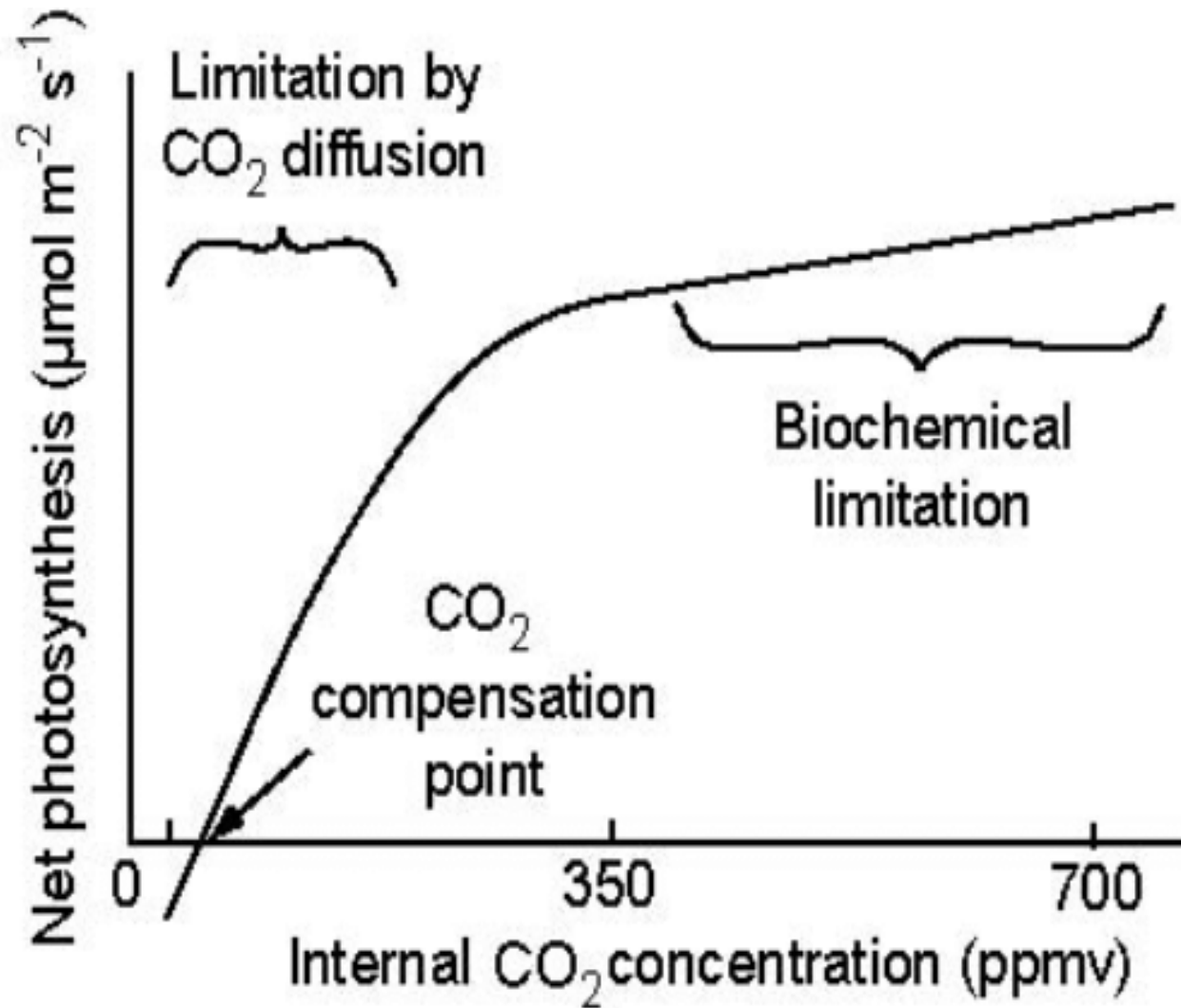


Trade off:  
Gain carbon  
and water  
loss

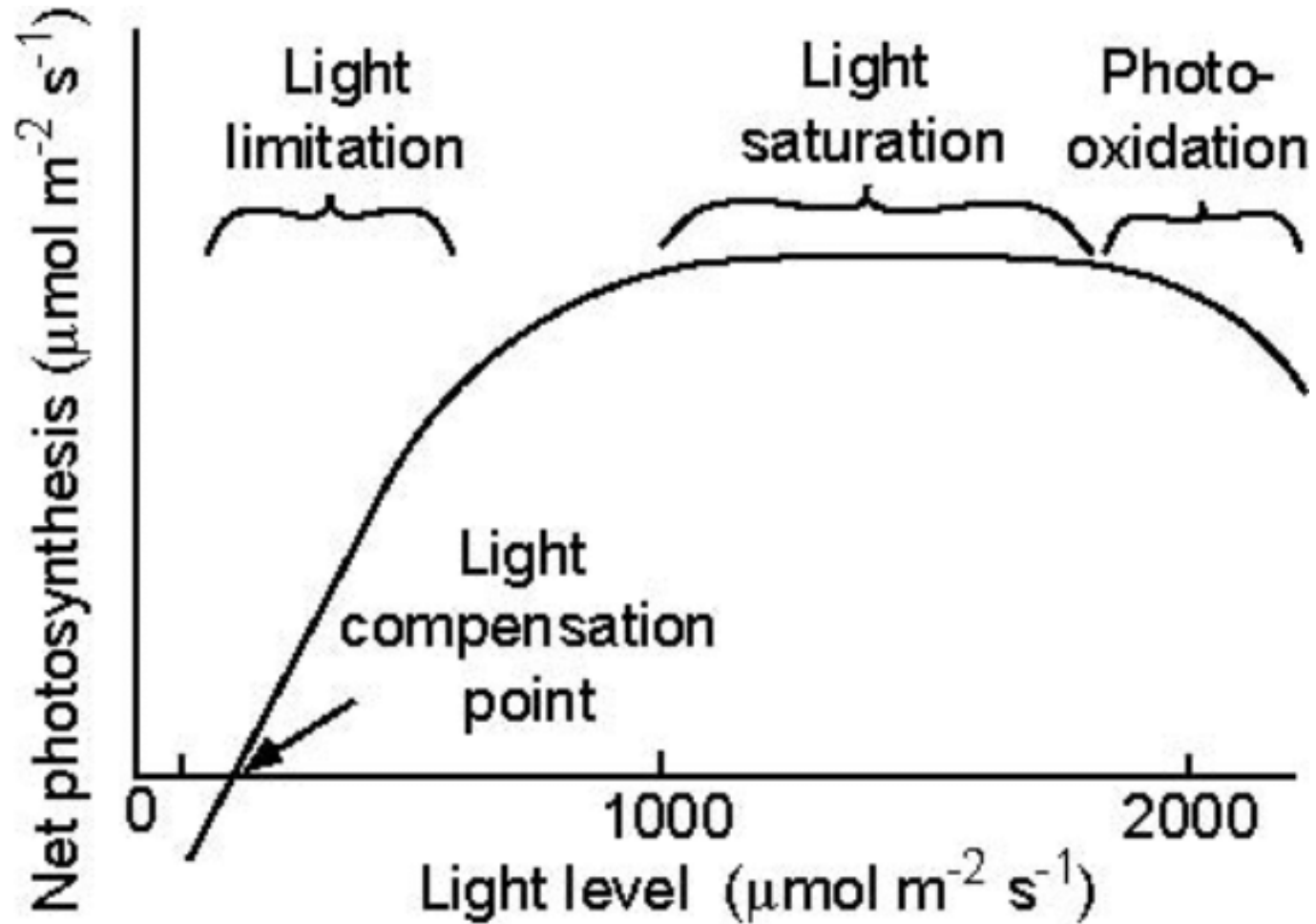




# CO<sub>2</sub> response curve of photosynthesis



# Light response curve of photosynthesis



# Calvin cycle

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## Photosynthesis

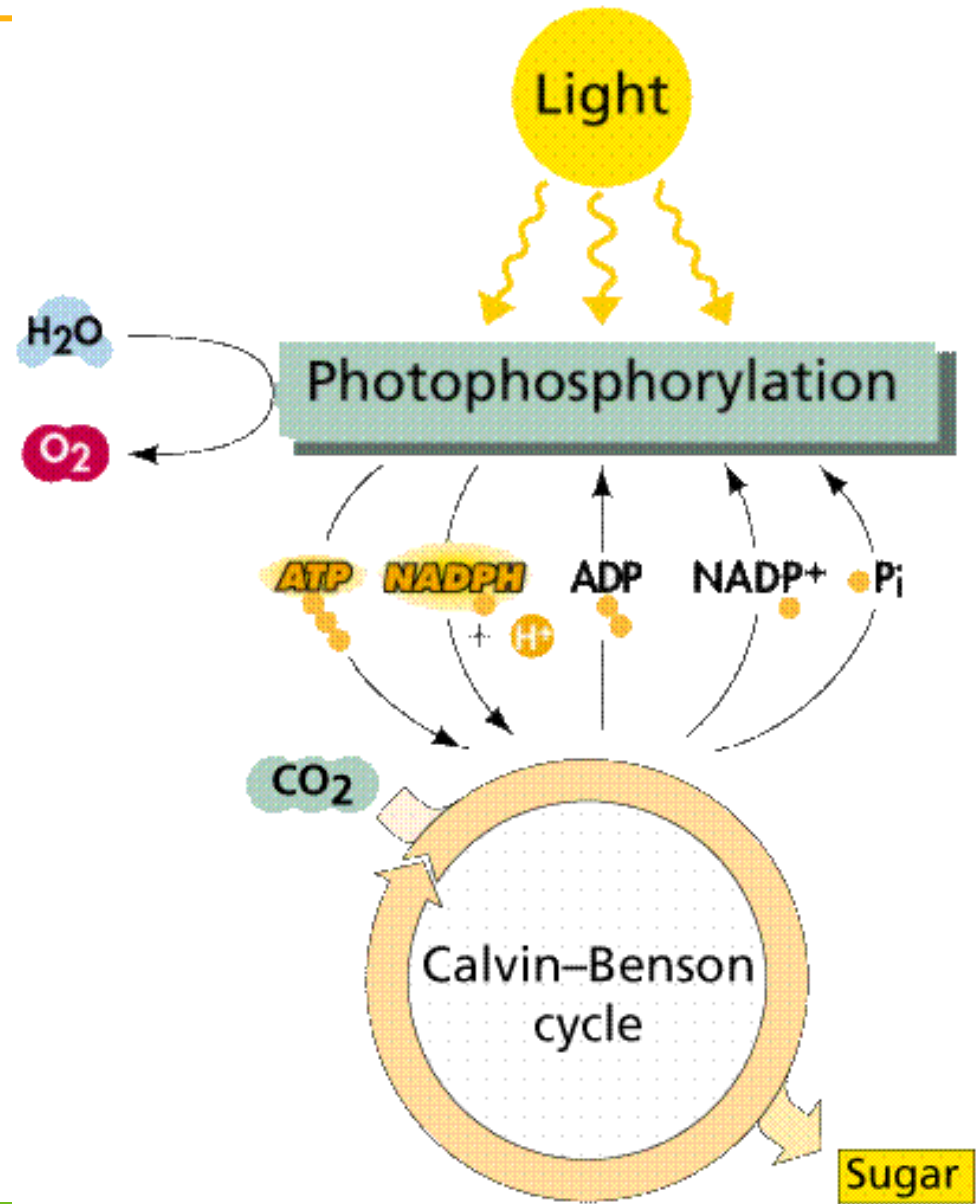
Two sets of reactions:

### Light harvesting

- converts light energy to chemical energy (ATP, NADPH)
- splits  $\text{H}_2\text{O}$  and produces  $\text{O}_2$  as byproduct

### Carbon fixing

- uses ATP and NADPH from light reactions to fix  $\text{CO}_2$  into sugar



## Models for photosynthesis

### 1. Empirical

#### - Light-use efficiency

Montieth 1977:

Biomass accumulation correlated with light interception

“Conversion efficiency” can be used to estimate gross primary production

Global estimates first used in CASA (Field et al. 1998, Sellers et al. 1992):

$$NPP = f(NDVI) \times PAR \times \epsilon^* \times g(T) \times h(W)$$

Later used in BIOME BGC and MODIS NPP models

**Limited to period of calibration**

### 2. Mechanistic

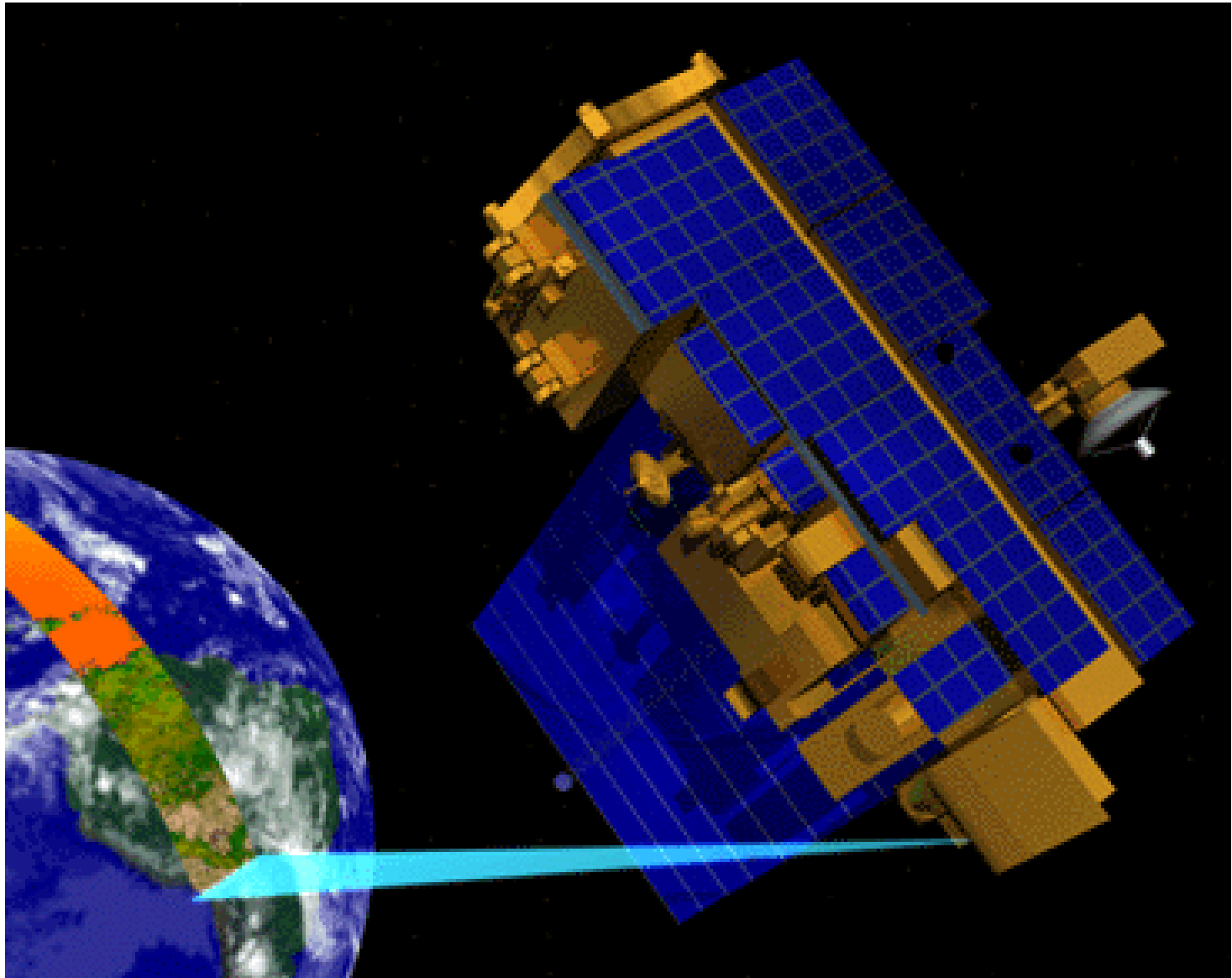
#### - Diffusion based

### 3. Semi-empirical

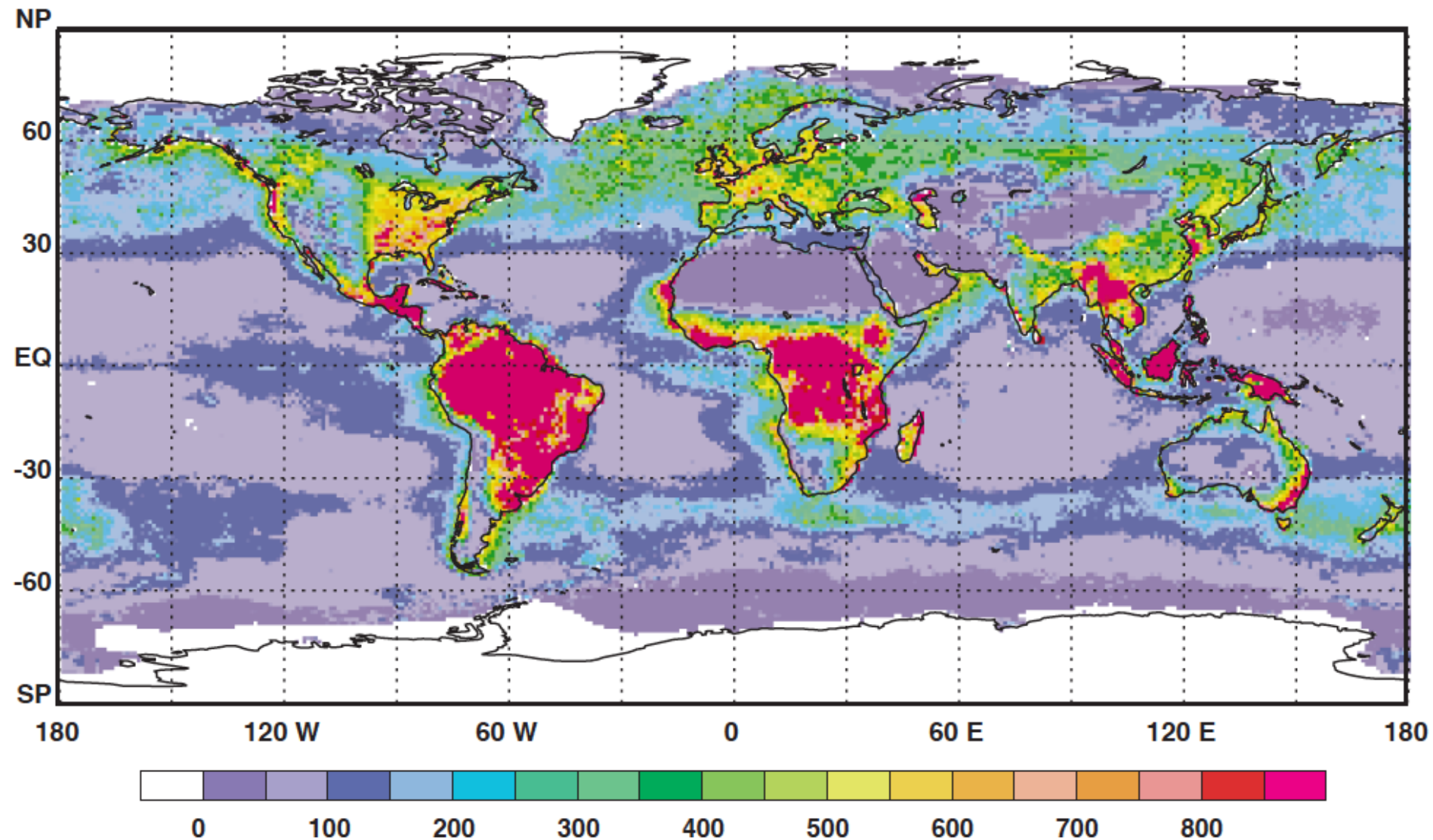
#### - Biochemical



# Carbon and water cycling



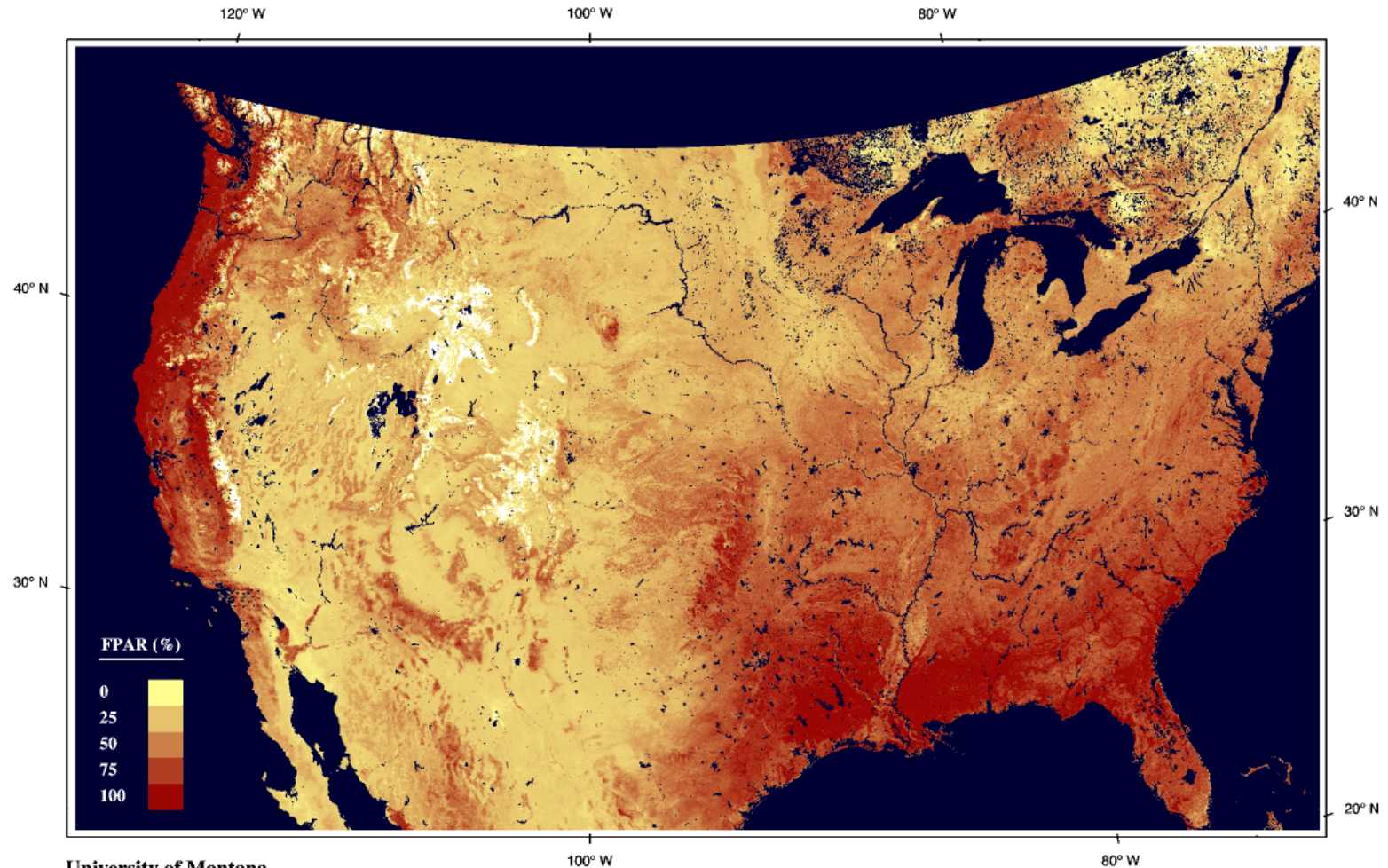
# Carbon and water cycling





# Carbon and water cycling

## MODIS FPAR (Fraction of Photosynthetically Active Radiation) Composite March 24 - April 8, 2000



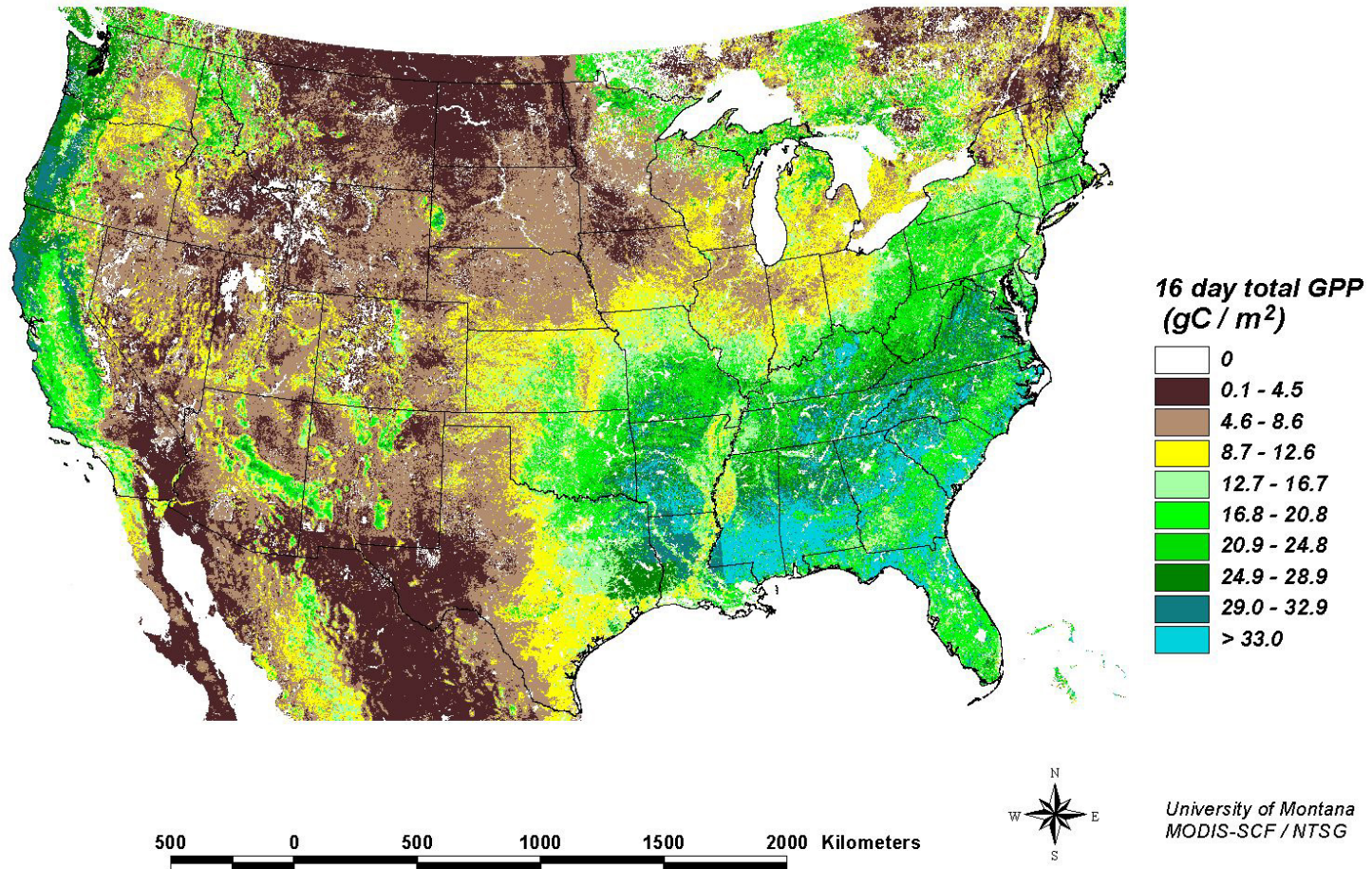
University of Montana  
Science Compute Facility





# Carbon and water cycling

United States  
MODIS Land Gross Primary Production  
16 day total, March 26 - April 10, 2000



## Models for photosynthesis

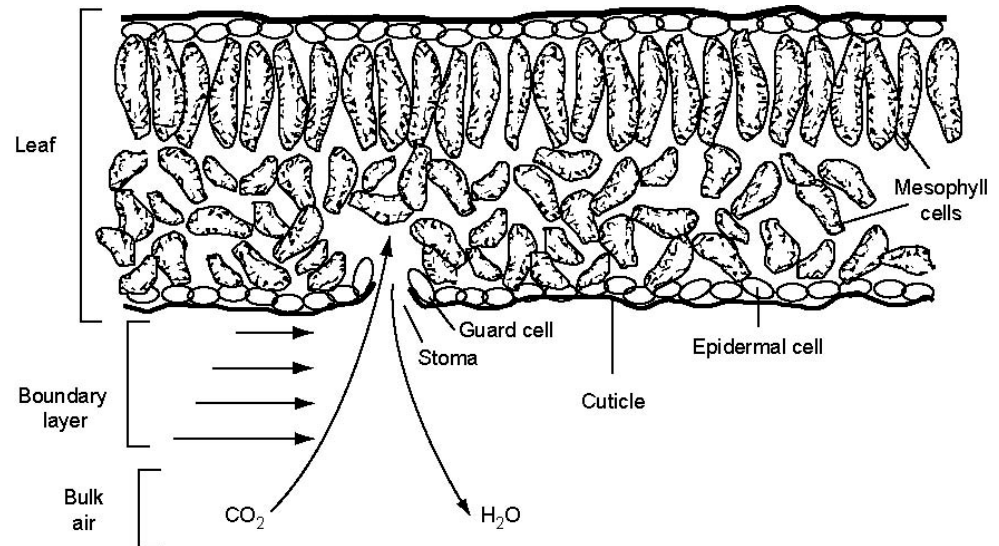
1. Empirical
  - Light-use efficiency

2. Mechanistic
  - Diffusion based

3. Semi-empirical
  - Biochemical

Fick's law of diffusion

$$A_{n,leaf} = g_c (C_{ca} - C_{ci})$$



Does not work well for low light & high humidity

## Models for photosynthesis

1. Empirical
  - Light-use efficiency

2. Mechanistic
  - Diffusion based

3. Semi-empirical
  - Biochemical

$$A = \min \left\{ \begin{array}{c} J_E \\ J_C \\ J_S \end{array} \right\}$$

$$J_E = \frac{\alpha_p e_m Q_p (C_{ci} - \Gamma^*)}{(C_{ci} - 2\Gamma^*)}$$

$$\Gamma^* = \frac{C_{oa}}{2\tau}$$

$$J_C = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$

$$J_S = V_m / 2$$

Farquhar 1980  
Collatz 1991



## Models for photosynthesis

1. Empirical
  - Light-use efficiency

$$V_m = \frac{V_{m,25} \exp[0.088(T_L - 25)]}{1 + \exp[0.29(T_L - 41)]}$$

2. Mechanistic
  - Diffusion based

$$A = \min \left\{ \begin{array}{c} J_E \\ J_C \\ J_S \end{array} \right\} \quad R_d = \frac{R_{d,25} \exp[0.069(T_L - 25)]}{1 + \exp[1.3(T_L - 55)]}$$

3. Semi-empirical
  - Biochemical

$$K_c, \tau, K_o, V_m, R_d$$

$$k = k_{25} \exp[q(T_L - 25)]$$



## Models for photosynthesis

$$A = \min \left\{ \begin{array}{c} J_E \\ J_C \\ J_S \end{array} \right\}$$

$$J_P = \frac{J_E + J_C - \sqrt{(J_E + J_C)^2 - 4\theta J_E J_C}}{2\theta}$$

$$A = \frac{J_P + J_S - \sqrt{(J_P + J_S)^2 - 4\beta J_P J_S}}{2\beta}$$

$$A_{net} = A - R_d$$

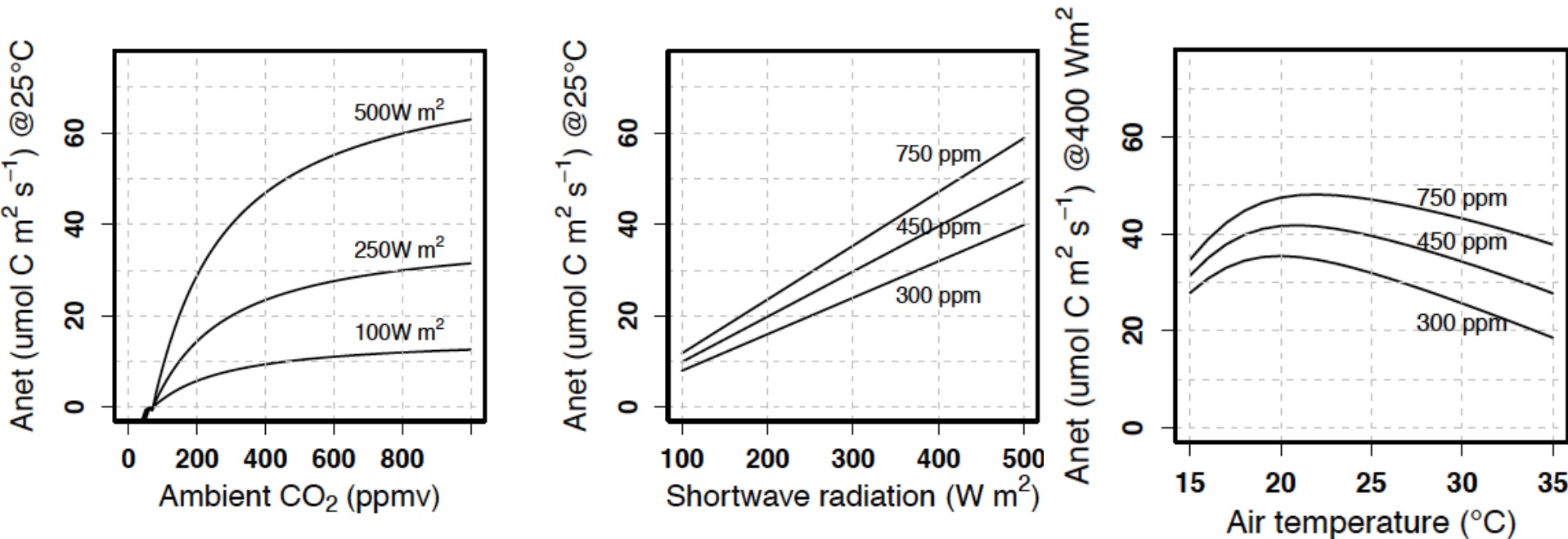
$$R_d = 0.015V_m$$

Co-limitation rather than sharp transition

- No co-limitation in ORCHIDEE
- Strong colimitation in LPJ (no Js)



## Biochemical model response curves



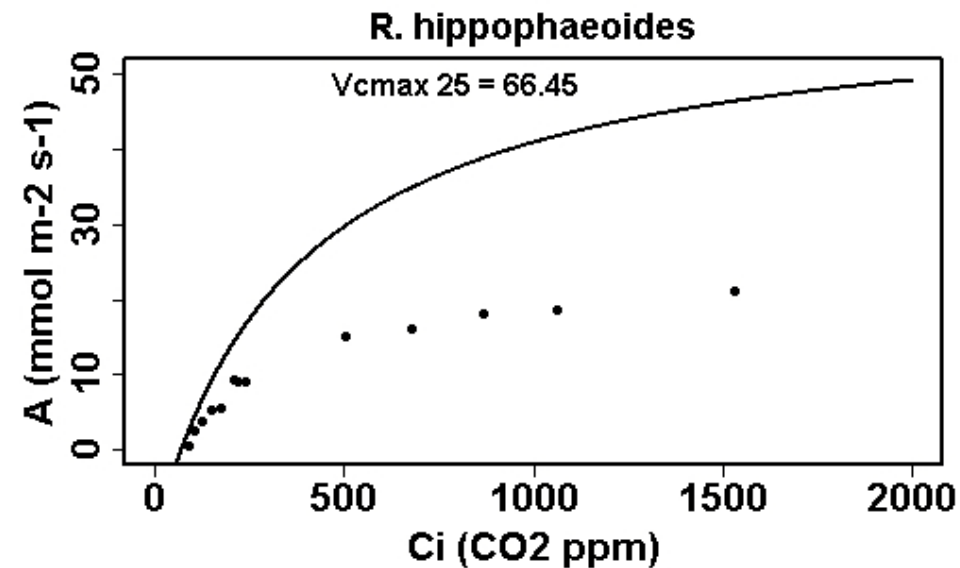


# Carbon and water cycling

## Vcmax

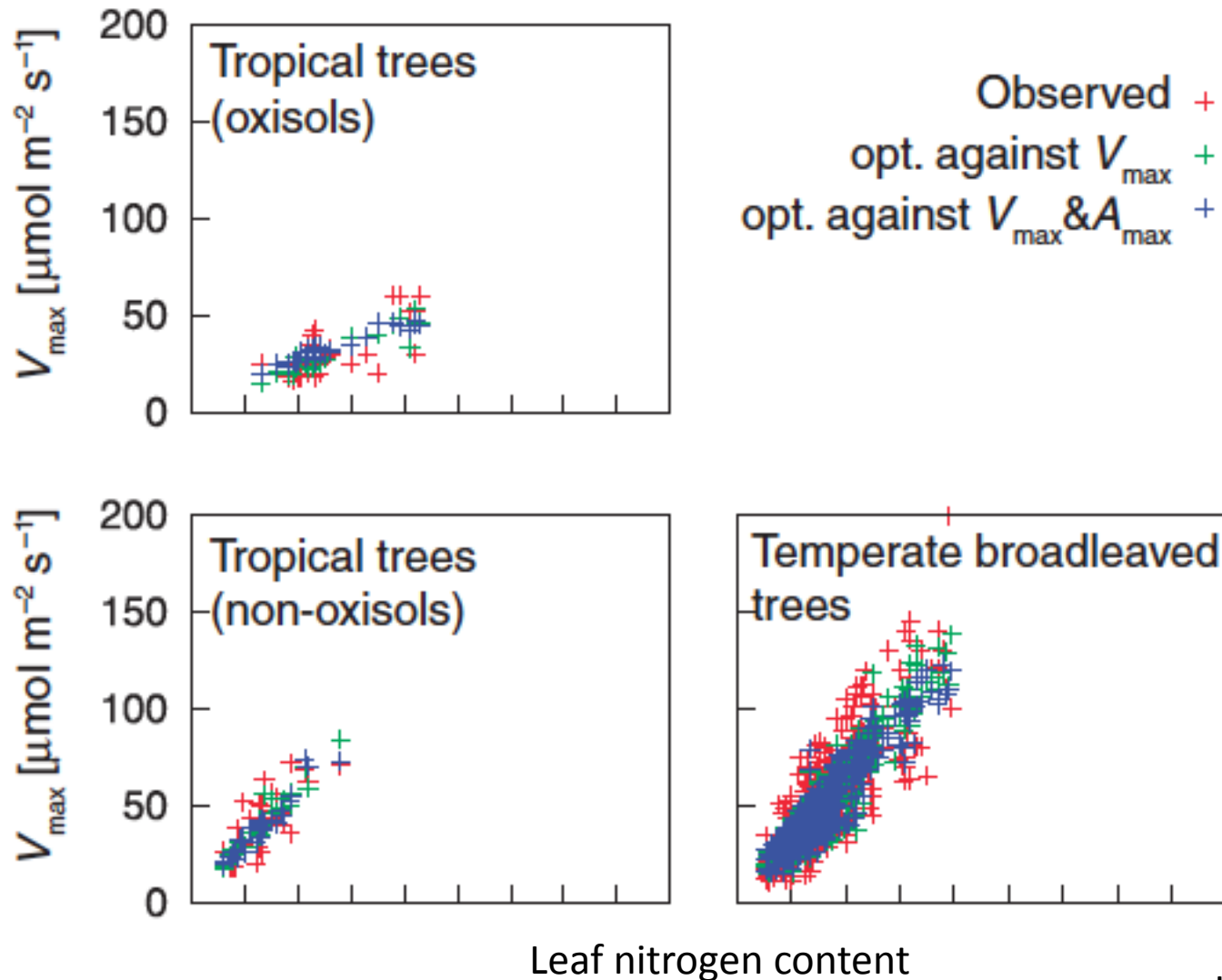
- Vcmax and Ci are needed
- Vcmax: Maximum rate of carboxylation
- Measure with:
  - Field measurements

$$J_C = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$





# Carbon and water cycling



Kattge 2009



# Carbon and water cycling

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## V<sub>c</sub>max

- V<sub>c</sub>max and C<sub>i</sub> are needed
- V<sub>c</sub>max: Maximum rate of carboxylation
- Measure with:
  - Field measurements
  - Modeled (Haxeltine and Prentice 1996)
    - Optimization algorithm based on evidence that N content and Rubisco activity vary vertically within the canopy and seasonally
    - Takes form of light-use efficiency model

$$J_c = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$

$$V_m = (1 / b_{C3}) (CI_{C3} / C2_{C3}) [(2\theta - 1)s - (2\theta s - C2_{C3})\sigma] \text{ APAR}$$



# Carbon and water cycling

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## Vcmax

- Vcmax and Ci are needed
- Vcmax: Maximum rate of carboxylation
- Measure with:
  - Field measurements
  - Modeled (Haxeltine and Prentice 1996)
  - Estimate from leaf nitrogen (Cox 1998)

$$J_c = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$

$$V_{c,\max} = n_2 N$$

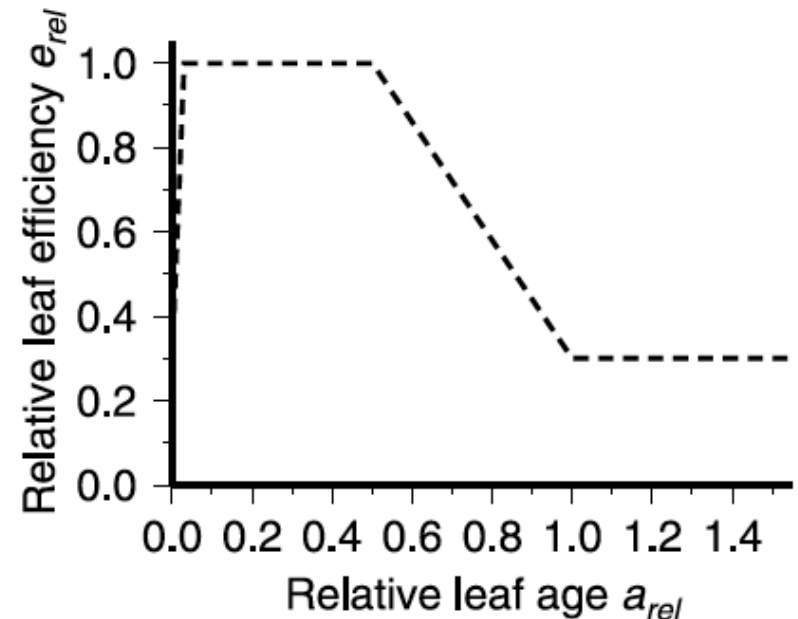


# Carbon and water cycling

## Vcmax

- Vcmax and Ci are needed
- Vcmax: Maximum rate of carboxylation
- Measure with:
  - Field measurements
  - Modeled (Haxeltine and Prentice 1996)
  - Estimate from leaf nitrogen (Cox 1998)
  - Prescribe from observation (Viovy 1996)
    - Modify for leaf age
    - Soil moisture
    - Canopy position (follow light extinction)

$$J_C = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$

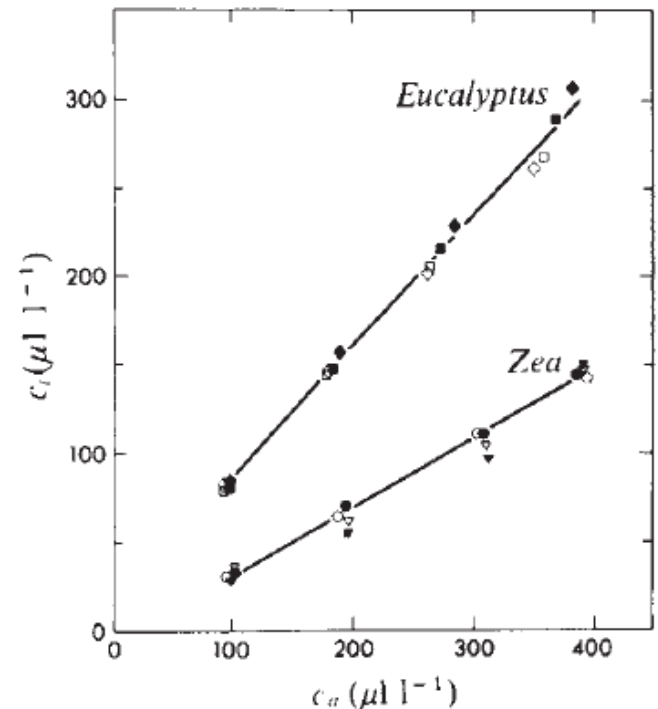
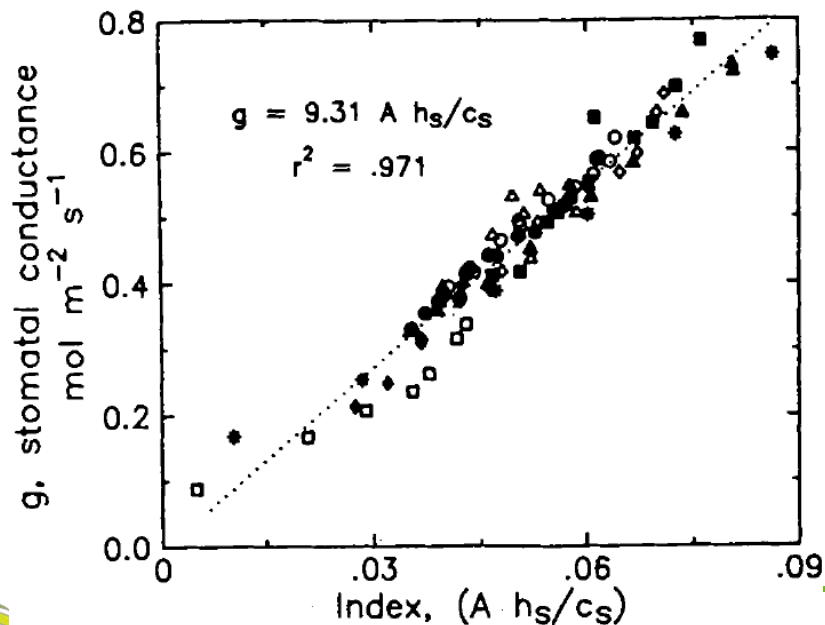


## Internal leaf $\text{CO}_2$ concentration

- Still need  $C_i$
- Depends on stomata and rate of photosynthesis
- Constant  $C_i/C_a$  (Wong 1979)
  - Suggests stomates optimize  $A / T$

$$J_C = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$

$$g_c = \frac{A_{n,leaf}}{(C_{ca} - C_{ci})}$$



## Internal leaf CO<sub>2</sub> concentration

- Still need C<sub>i</sub>
- Depends on stomata and rate of photosynthesis
- Constant C<sub>i</sub>/C<sub>a</sub> (Wong 1979)
  - Suggests stomates optimize A / T

$$J_c = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$

$$A_{n,leaf} = g_c (C_{ca} - C_{ci}) \quad \rightarrow \quad C_{ci} = \frac{A_{n,leaf}}{g_c} + C_{ca}$$

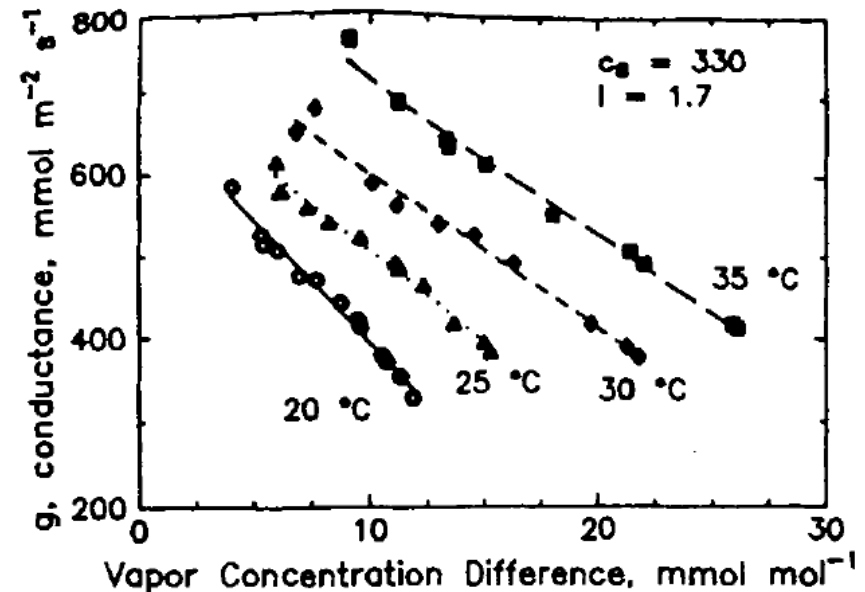


## Internal leaf CO<sub>2</sub> concentration

- Conductance model is required to relate assimilation and stomatal conductance to the gradient of CO<sub>2</sub> between the atmosphere and Rubisco
- Stomata respond to:
  - Light
  - CO<sub>2</sub>
  - Humidity
  - VPD
  - Soil moisture
- Ball-Berry model:

$$g_{cs} = m \frac{A_n h_s}{C_{cs}} + b$$

$$J_C = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$



Ball et al. 1987





## Internal leaf CO<sub>2</sub> concentration

- Conductance model is required to relate assimilation and stomatal conductance to the gradient of CO<sub>2</sub> between the atmosphere and Rubisco
- Stomata respond to:
  - Light
  - CO<sub>2</sub>
  - Humidity
  - VPD
  - Soil moisture
- Simultaneous solution for A, C<sub>i</sub>, and G<sub>c</sub>

$$J_C = \frac{V_m (C_{ci} - \Gamma^*)}{C_{ci} + K_c (1 + C_{oa} / K_o)}$$

$$g_{cs} = m \frac{A_n h_s}{C_{cs}} + b$$

$$A_{n,leaf} = g_c (C_{ca} - C_{ci})$$

$$A_{net} = A - R_d$$



## Model application

- ORCHIDEE
  - Farquhar photosynthesis
    - $V_{max}$  – age and soil moisture limited
  - Ball-Berry conductance model
    - No direct soil moisture limitation

**Table 1.** PFTs and PFT-Specific Parameters in ORCHIDEE<sup>a</sup>

PFT	$V_{cmax,opt}$	$T_{opt}$	$\lambda_{max}$	$z_{root}$	$\alpha_{leaf}$	$h$	$A_c$	$T_s$	$H_s$
TrBE	50	37	10	1.25	0.12	25	910	-	0.3
TrBR	60	37	10	1.25	0.14	25	180	-	0.3
TeNE	37.5	27	5	1.	0.14	15	910	-	-
TeBE	37.5	32	5	1.25	0.14	15	730	-	-
TeBS	37.5	28	5	1.25	0.14	15	180	12.5	-
BoNE	37.5	25	4.5	1.	0.14	10	910	-	-
BoBS	37.5	25	4.5	1.	0.14	10	180	5	-
BoNS	35	25	4	1.25	0.14	10	180	7	-
NC3	70	$27.5 + 0.25T_l$	2.5	0.25	0.20	0.2	120	4	0.2
NC4	70	36	2.5	0.25	0.20	0.2	120	5	0.2
AC3	90	$27.5 + 0.25T_l$	6	0.25	0.18	0.4	150	10	0.2
AC4	90	36	3	0.25	0.18	0.4	120	10	0.2



# Carbon and water cycling

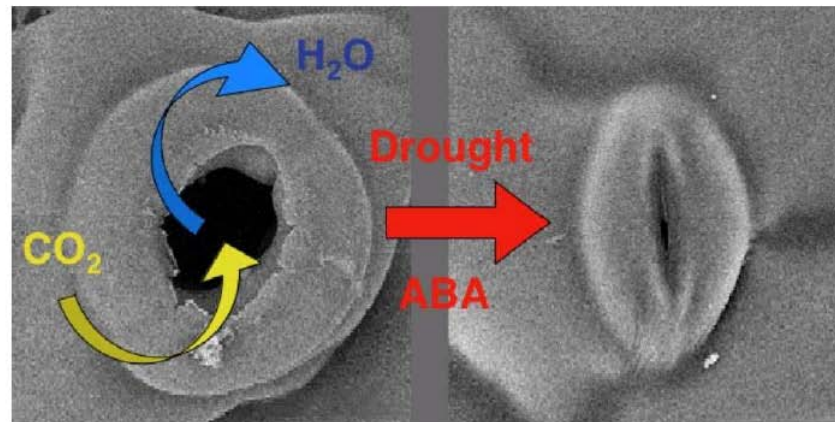
## Model application

Symbol	Value	Units	$Q_{10}$	Description
$K_c$ $\text{CO}_2$	30 <sup>a</sup>	Pa	2.1	Michaelis constant for
$K_o$	30 <sup>a</sup>	kPa	1.2	Michaelis constant for $\text{O}_2$
$\tau$	2600 <sup>b</sup>		0.57	$\text{CO}_2/\text{O}_2$ specificity ratio
$\alpha_{\text{C3}}$	0.08 <sup>a</sup>			$\text{C}_3$ quantum efficiency
$b_{\text{C3}}$	0.015 <sup>c</sup>			$R_d/V_m$ ratio for $\text{C}_3$ plants
$\lambda_{\text{mC3}}$	0.7 <sup>d</sup>			optimal $c_i/c_a$ for $\text{C}_3$ plants
$\alpha_{\text{C4}}$	0.053 <sup>c</sup>			$\text{C}_4$ quantum efficiency
$b_{\text{C4}}$	0.035			$R_d/V_m$ ratio for $\text{C}_4$ plants
$\lambda_{\text{mC4}}$	0.4			optimal $c_i/c_a$ for $\text{C}_4$ plants
$\alpha_a$	0.5			scaling parameter for $\alpha$
$c_a$	340	$\mu\text{mol mol}^{-1}$		ambient mole fraction $\text{CO}_2$
$P$	100	kPa		atmospheric pressure
$\text{O}_2$	20.9	kPa		partial pressure $\text{O}_2$
$C_{\text{mass}}$	12	$\text{g mol}^{-1}$		molar mass of carbon
$k$	0.5 <sup>f</sup>			extinction coefficient
$\theta$	0.7 <sup>g</sup>			co-limitation parameter



## Model application

- LPJ
  - Farquhar photosynthesis
    - No soil moisture limitation
  - Haxeltine conductance model
    - If not enough soil moisture to sustain potential conductance,  $G_c$  is reduced, and  $C_i$  is reduced



Stomata in plant leaves

[www.isv.cnrs-gif.fr/jg/images/stomata.jpg](http://www.isv.cnrs-gif.fr/jg/images/stomata.jpg)

## Scaling from leaves to canopies

- Real canopies

- LAI gradients
- Leaf angle
- Shade/sun
- N gradients
- Light gradients
- ...

$$FPAR = 1 - \exp(-k \text{ LAI})$$

$$N_0 = N_{can} k / f_{PAR}$$

$$A_{can} = A_0 f_{PAR} / k$$

- Big leaf: assumes that canopy carbon fluxes have the same relative responses to the environment as any single leaf, and that the scaling from leaf to canopy is therefore linear.

- Beer's Law
  - Integrate over vertical canopy layers

- Two-layer:

- Sun – shade division
- Diffuse vs direct light



## Take home message

- Coupled approach must be used to model photosynthesis (Anet)
  - $G_c$
  - $C_i$
- Leaf to canopy scaling requires integration over non-linear processes
- Move beyond semi-empirical approaches
  - Medlyn 2011
- Plenty of uncertainties to explore
  - Temperature sensitivities
  - Light sensitivities
  - $CO_2$  sensitivities
  - Nutrient sensitivities
  - $V_{cmax}$
  - Vertical canopy gradients

$$E - \lambda A$$



# Carbon and water cycling

## Recommended reading

- Books
  - An introduction to environmental biophysics (Campbell and Norman 1998)
  - Physicochemical and Environmental Plant Physiology (Nobel 1999)
- Some papers
  - Wong, S. and I. F. Cowan, G. (1979). "Stomatal conductance correlates with photosynthetic capacity." Nature **282**: 424-426.
  - Farquhar, G. D., S. von Caemmerer, et al. (1980). "A biochemical model of photosynthetic CO<sub>2</sub> assimilation in leaves of C<sub>3</sub> species." Planta **149**: 78-90.
  - Collatz, G. J., J. T. Ball, et al. (1991). "Physiological and environmental regulation of stomatal conductance, photosynthesis and transpiration: A model that includes a laminar boundary layer." Agricultural and Forest Meteorology **54**: 107-136.
  - Sellers, P. J., J. A. Berry, et al. (1992). "Canopy reflectance, photosynthesis, and transpiration. III. A reanalysis using improved leaf models and a new canopy integration scheme." Remote Sensing of Environment **42**: 187-216. Friend, A. D. (2001). "Modelling canopy CO<sub>2</sub> fluxes: Are 'Big-Leaf' simplifications justified?" Global Ecology and Biogeography **10**(6): 603-619.
  - Damour, G., T. Simonneau, et al. (2010). "An overview of models of stomatal conductance at the leaf level." Plant, Cell and Environment **33**: 1419-1438.
  - Medlyn, B. E., R. A. Duursma, et al. (2011). "Reconciling the optimal and empirical approaches to modelling stomatal conductance." Global Change Biology: doi: 10.1111/j.1365-2486.2010.02375.x.

