



PEKING  
UNIVERSITY

# The long road towards realistic CO<sub>2</sub> flux maps from satellite column retrievals

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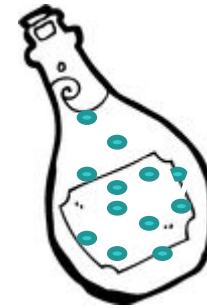
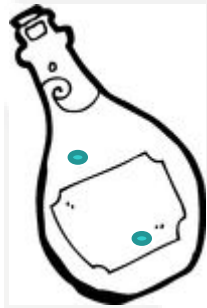


LABORATOIRE DES SCIENCES DU CLIMAT & DE L'ENVIRONNEMENT



# Mapping CO<sub>2</sub> sources and sinks

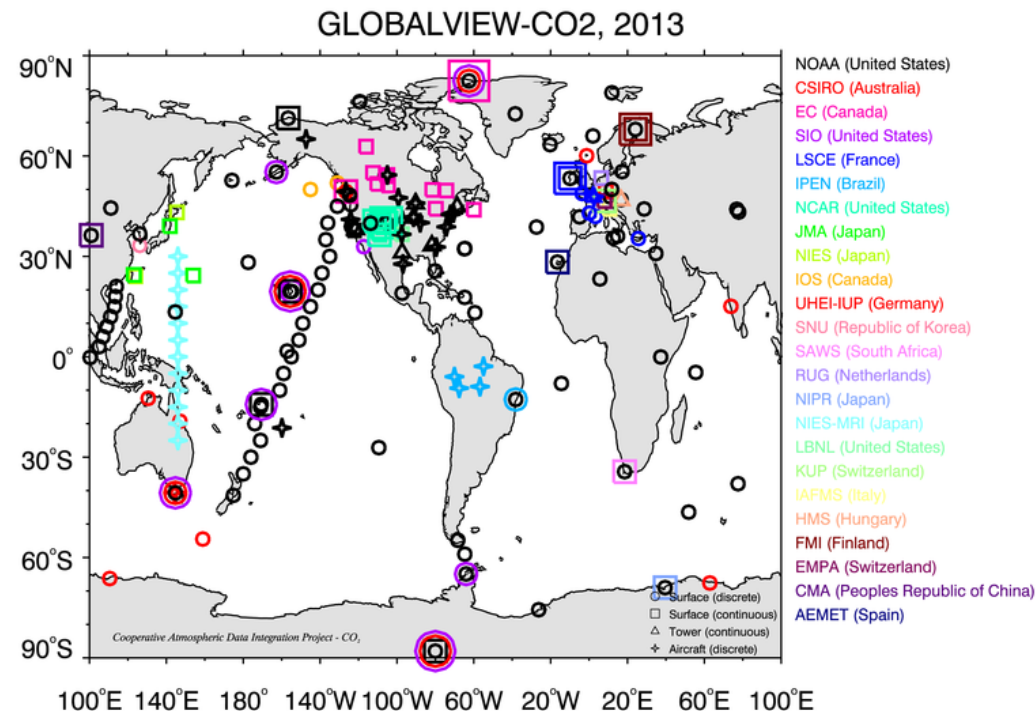
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Atmospheric inversion

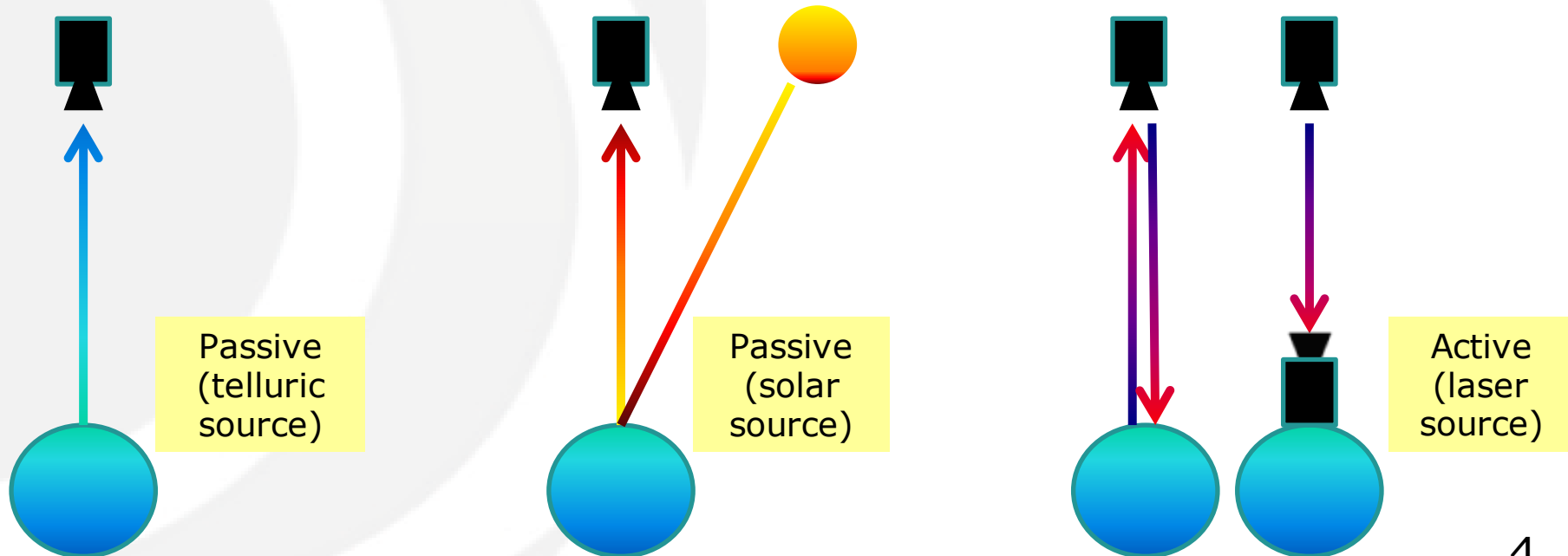
# Air sample measurements

- Measurements to monitor CO<sub>2</sub> at the Earth's surface are usually accurate to within 1 ‰ for multi-year means.
  - This specification **penalises their spread over the globe.**



# CO<sub>2</sub> remote sensing from space

- Measuring CO<sub>2</sub> indirectly from its radiative effect.
- CO<sub>2</sub> signal is in competition with that of clouds, aerosols, etc.
- Massive volume of measurements.
  - No sounding in the presence of thick clouds or in the absence of source.




# Stringent accuracy requirements for CO<sub>2</sub> column retrievals

Needs for CO<sub>2</sub> flux inversion, given the amplitude of the expected signal:

- Random errors < 2%.
- Systematic errors < 1.25 ‰ (3 ‰ pour CH<sub>4</sub>).

Very ambitious for satellite measurements.

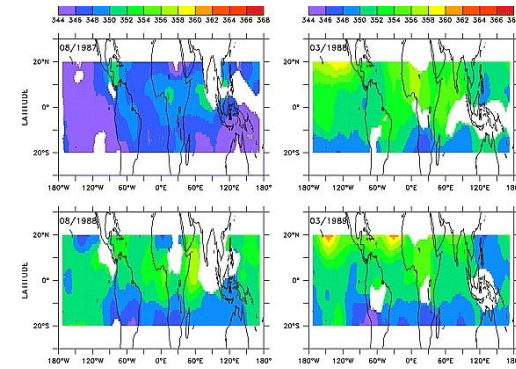
	ESA Climate Change Initiative (CCI)		Page 14
	<b>User Requirements Document</b>		Version 2 –
	<b>Version 2 (URDv2)</b>		Final
	for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)		28 August 2014

Requirements for regional CO <sub>2</sub> and CH <sub>4</sub> source/sink determination					
Parameter	Req. type	Random error ("Precision")		Systematic error	Stability
		Single obs.	1000 <sup>2</sup> km <sup>2</sup> monthly		
XCO <sub>2</sub>	G	< 1 ppm	< 0.3 ppm	< 0.2 ppm (absolute)	As systematic error but per year
	B	< 3 ppm	< 1.0 ppm	< 0.3 ppm (relative <sup>§1</sup> )	–
	T	< 8 ppm	< 1.3 ppm	< 0.5 ppm (relative <sup>§1</sup> )	–
XCH <sub>4</sub>	G	< 9 ppb	< 3 ppb	< 1 ppb (absolute)	As systematic error but per year
	B	< 17 ppb	< 5 ppb	< 5 ppb (relative <sup>§1</sup> )	–
	T	< 34 ppb	< 11 ppb	< 10 ppb (relative <sup>§1</sup> )	–

Table 1: GHG-CCI XCO<sub>2</sub> and XCH<sub>4</sub> random ("precision") and systematic retrieval error requirements for measurements over land. Abbreviations: G=Goal, B=Breakthrough, T=Threshold requirement. <sup>§1</sup> Required systematic error after an empirical bias correction, that does not use the verification data. <sup>§2</sup> Required systematic error and stability after bias correction, where bias correction is not limited to the application of a constant offset / scaling factor.

# Growing investment from the space agencies

- Partial column products from non-CO<sub>2</sub>-dedicated missions:
  - TOVS, AIRS, IASI, TES.
- Total column products from CO<sub>2</sub>-dedicated missions:
  - Japan:
    - GOSAT (JAXA/NIES/MoE), launched in 2009.**
    - GOSAT-2 (JAXA/NIES/MoE), planned for 2018.**
  - USA:
    - OCO (NASA), failed launch in 2009.**
    - OCO-2 (NASA), launched in 2014.**
  - China:
    - TanSat (CAS, MOST, CMA) planned for 2015.**
  - Europe:
    - Sciamachy (ESA), 2002-2012.**
  - More satellites are under study (US ASCENDS, France Microcarb, etc.).

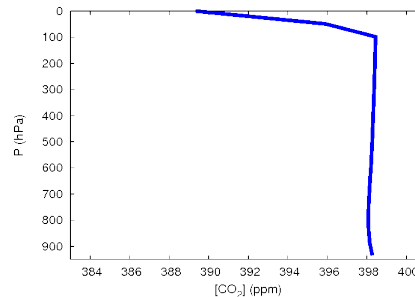


Chédin et al., *JGR*, 2003.  
First satellite CO<sub>2</sub> retrievals (upper-trop. and Tropics)

# CO<sub>2</sub> remote sensing

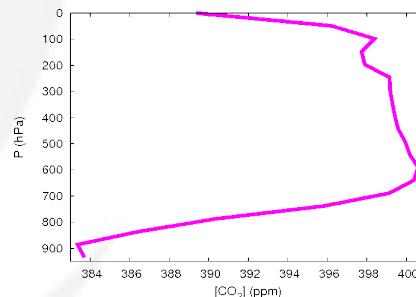
- The estimation problem is under-constrained: **we complete the measurements with a priori information**. The fusion of probabilistic information is rigorously expressed by Bayes' theorem.

A priori [CO<sub>2</sub>]  
+  
uncertainties.

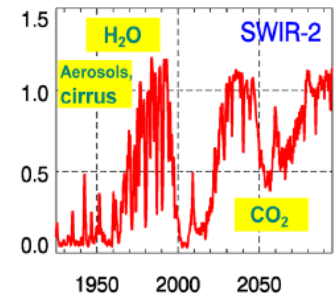


$$p(\mathbf{x}|\mathbf{y}) = \frac{p(\mathbf{x}).p(\mathbf{y}|\mathbf{x})}{p(\mathbf{y})}$$

Estimated  
[CO<sub>2</sub>]  
+  
uncertainties.



CO<sub>2</sub> Profiles: OCO-2



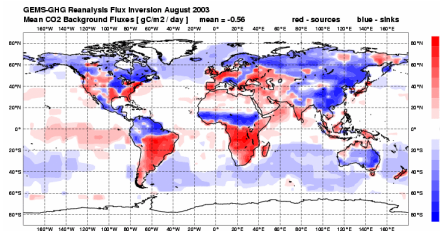
Observations  
+ uncertainties

- measurements (radiances),
- Radiation model.

# Atmospheric inversions

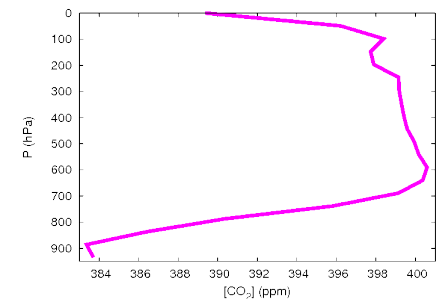
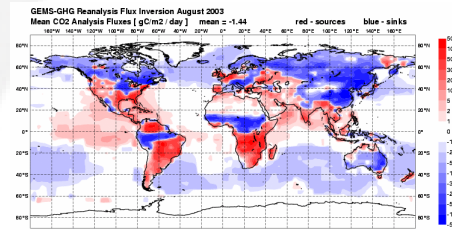
- The estimation problem is under-constrained: **we complete the measurements with a priori information**. The fusion of probabilistic information is rigorously expressed by Bayes' theorem.

A priori fluxes  
+  
uncertainties.



$$p(\mathbf{x}|\mathbf{y}) = \frac{p(\mathbf{x}).p(\mathbf{y}|\mathbf{x})}{p(\mathbf{y})}$$

Estimated  
fluxes  
+  
uncertainties.



Observations  
+ uncertainties

- of measurements,
- of chem.-transport model.



# Processing chain of the satellite measurements

- Level 0 product: Raw measurements



- L1: Calibrated measurements expressed in terms of radiances



$$p(\mathbf{x}|\mathbf{y}) = \frac{p(\mathbf{x}) \cdot p(\mathbf{y}|\mathbf{x})}{p(\mathbf{y})}$$

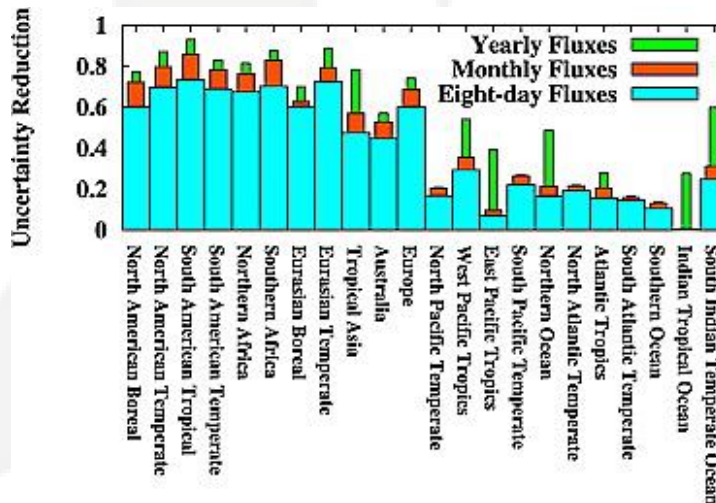
- L2: Profiles or columns of CO<sub>2</sub>



$$p(\mathbf{x}|\mathbf{y}) = \frac{p(\mathbf{x}) \cdot p(\mathbf{y}|\mathbf{x})}{p(\mathbf{y})}$$

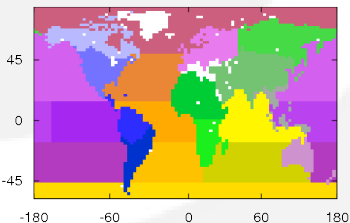
- L4: Maps of sources and sinks of CO<sub>2</sub>

We expect the end product to significantly increase our knowledge about CO<sub>2</sub> surface fluxes.



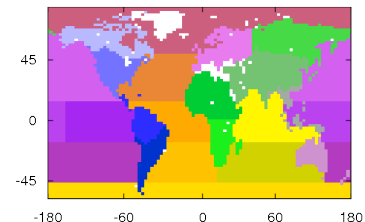
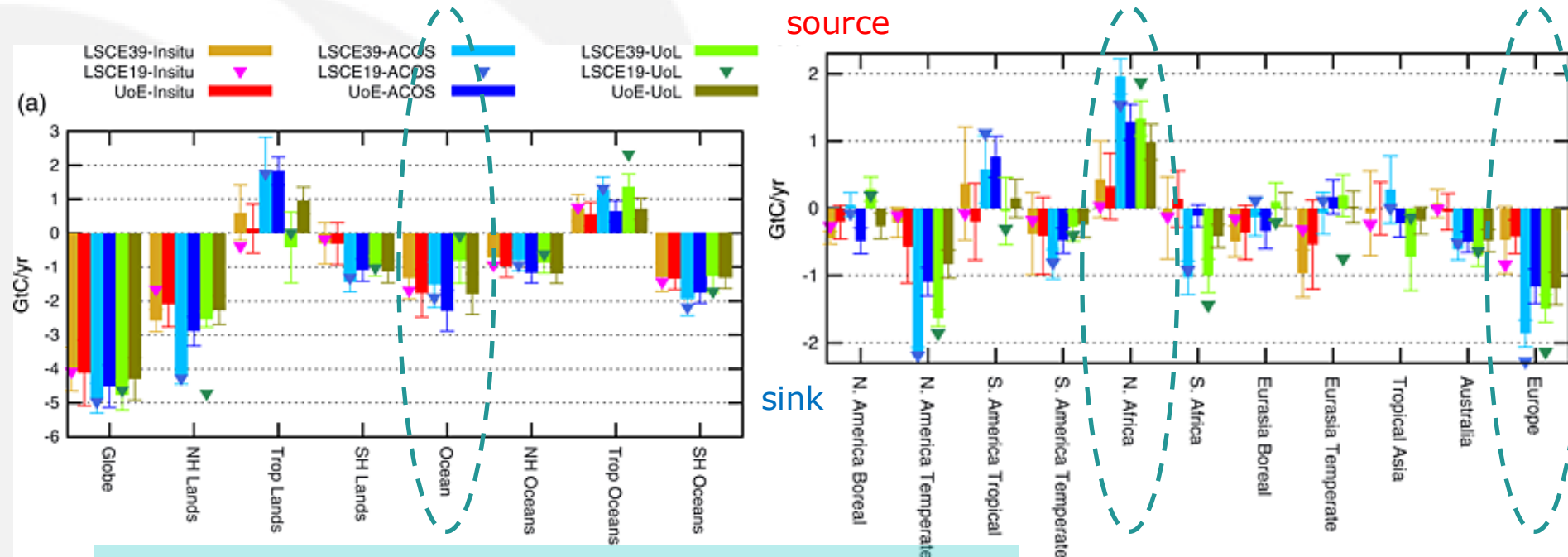
Theoretical uncertainty reduction for the GOSAT satellite  
(0=neutral; 1=perfect)

Chevallier et al. (*GRL*, 2009)



# Spread and biased GOSAT CO<sub>2</sub> global inversions (1/2)

- 2 GOSAT products or surface air sample measurements (2010), 2 inversion systems, 2 versions of 1 of the transport models.

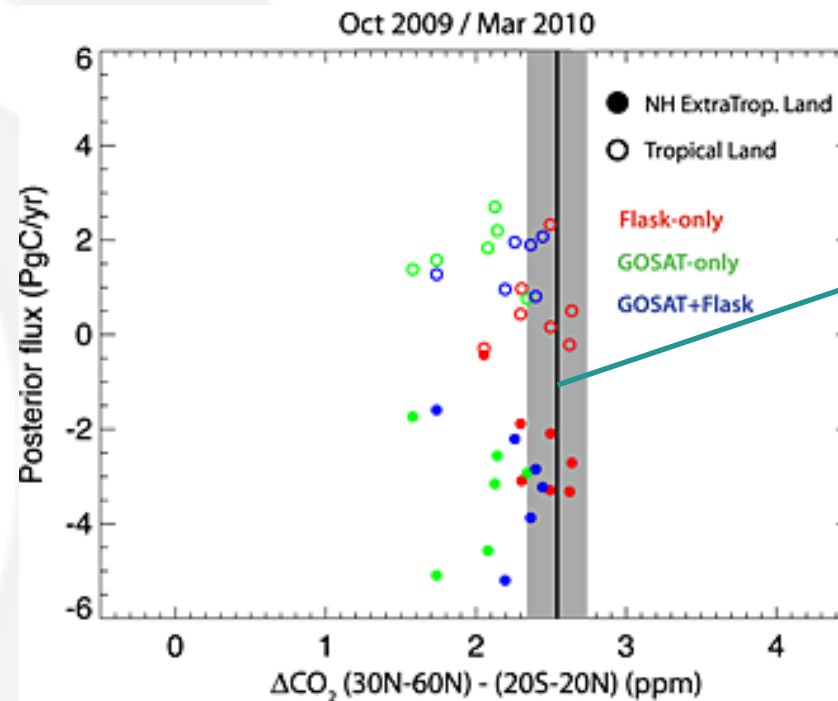


# Spread and biased GOSAT CO<sub>2</sub> global inversions (2/2)

- Aircraft measurement campaigns in the Pacific do not support the CO<sub>2</sub> meridional gradient inferred by the GOSAT retrievals.

Comparison between simulated and measured meridional gradients of CO<sub>2</sub>, and their relationship with inversion-derived carbon fluxes.

Houweling et al.  
(*JGR*, 2015)



Mean and range of meridional gradients that are supported by HIPPO aircraft measurements between 900 hPa and 300 hPa collected during HIPPO 2 (Oct. 2009) and HIPPO 3 (Mar. 2010).

$\Delta\text{CO}_2$  denotes the difference in CO<sub>2</sub> between 30°N–60°N and 20°S–20°N.

# Processing chain

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L0 (raw measurements)



L1 (calibrated radiances)



$$p(\mathbf{x}|\mathbf{y}) = \frac{p(\mathbf{x}) \cdot p(\mathbf{y}|\mathbf{x})}{p(\mathbf{y})}$$

L2 (CO<sub>2</sub> retrievals)



$$p(\mathbf{x}|\mathbf{y}) = \frac{p(\mathbf{x}) \cdot p(\mathbf{y}|\mathbf{x})}{p(\mathbf{y})}$$

L4 (CO<sub>2</sub> fluxes)

- The steps are spread between various institutes.
- Is the resulting chain consistent from end to end?
- Only mitigation measure so far: averaging kernels **KH** (linear representation of the weighting of information content of the retrieval).

- $\mathbf{x}^{sim} = \mathbf{x}^b + \mathbf{KH}(\mathbf{x}^{model} - \mathbf{x}^b)$

**x**: retrieval vector (mostly CO<sub>2</sub> profile)

**x<sup>b</sup>**: retrieval prior of **x**

**x<sup>model</sup>**: direct model output

**x<sup>sim</sup>**: model-equivalent of **x**

**K**: retrieval gain matrix

**H**: linear retrieval observation

operator (mostly radiation model)

# Processing chain

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- From satellite radiances to **CO<sub>2</sub> retrievals** (using a radiation model **H**).
  - Optimal state  $\mathbf{x}^a = \mathbf{x}^b + \mathbf{K}(\mathbf{y} - \mathbf{H}\mathbf{x}^b)$  (1)
  - $\mathbf{K} = \mathbf{B}\mathbf{H}^T(\mathbf{H}\mathbf{B}\mathbf{H}^T + \mathbf{R})^{-1}$
  - Uncertainty  $\mathbf{A} = (\mathbf{I} - \mathbf{K}\mathbf{H}) \mathbf{B}$

**y**: observation vector  
**B**: prior error covariance matrix  
**R**: observation error covariance matrix
  
- From **CO<sub>2</sub> retrievals** to **estimated fluxes** (using a transport model **H** and – indicated with primes – the averaging kernel **KH**).
  - Optimal state  $\mathbf{x}^a = \mathbf{x}^b + \mathbf{K}'(\mathbf{y}' - \mathbf{H}'\mathbf{x}^b)$  (2)
  - $= \mathbf{x}^b + \mathbf{K}'(\mathbf{K}\mathbf{y} - \mathbf{K}\mathbf{H}\mathbf{H}\mathbf{x}^b)$  (3)
  - $= \mathbf{x}^b + \mathbf{K}'\mathbf{K}(\mathbf{y} - \mathbf{H}\mathbf{H}\mathbf{x}^b)$  (4)
  - $\mathbf{K}' = \mathbf{B}\mathbf{H}'^T(\mathbf{H}'\mathbf{B}\mathbf{H}'^T + \mathbf{R})^{-1}$  , with  $\mathbf{H}' = \mathbf{K}\mathbf{H}\mathbf{H}$
  - Uncertainty  $\mathbf{A} = (\mathbf{I} - \mathbf{K}'\mathbf{H}') \mathbf{B}$

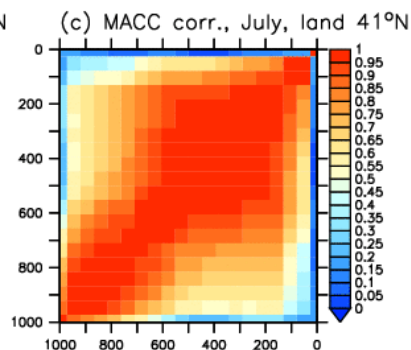
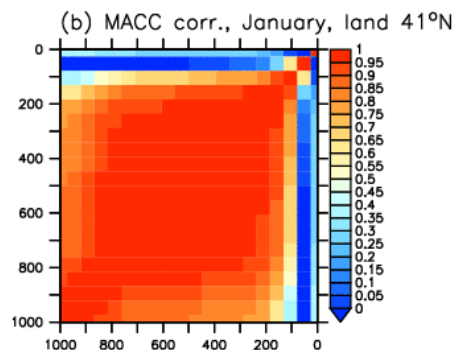
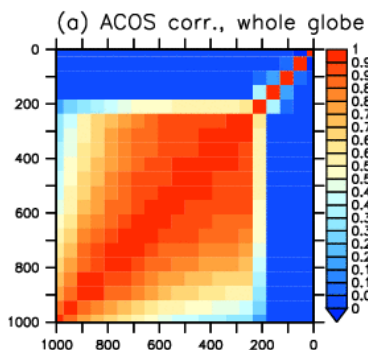
# Gain matrices $\mathbf{K}$

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- From  $\text{CO}_2$  retrievals to estimated fluxes.
- $\mathbf{K}'\mathbf{K} = \mathbf{B}\mathbf{H}'^T(\mathbf{H}'\mathbf{B}\mathbf{H}'^T + \mathbf{R})^{-1} \mathbf{B}\mathbf{H}^T(\mathbf{H}\mathbf{B}\mathbf{H}^T + \mathbf{R})^{-1}$
- We want this product to be a gain matrix itself so that:
  - $\mathbf{K}'\mathbf{K} = \mathbf{B}\mathbf{H}^T\mathbf{H}^T(\mathbf{H}\mathbf{H}\mathbf{B}\mathbf{H}^T\mathbf{H}^T + \mathbf{R})^{-1}$
- If  $\mathbf{H} \neq \mathbf{I}$ , we need:
  1.  $\mathbf{H}\mathbf{B}\mathbf{H}^T = \mathbf{H}\mathbf{H}\mathbf{B}\mathbf{H}^T\mathbf{H}^T$   
-> consistent prior error statistics in radiance space
  2.  $\mathbf{H}^T\mathbf{K}^T(\mathbf{K}\mathbf{H}\mathbf{B}\mathbf{H}^T\mathbf{K}^T + \mathbf{R})^{-1} \mathbf{B} = \mathbf{I}$   
->  $\mathbf{K}\mathbf{H} \approx \mathbf{I}$

# Consistent prior error statistics?

## Correlations

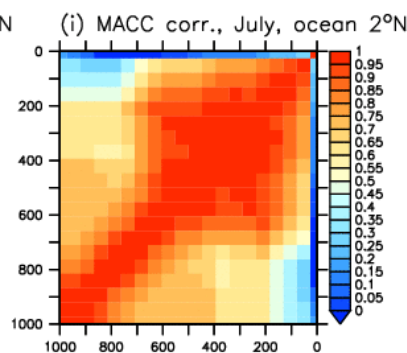
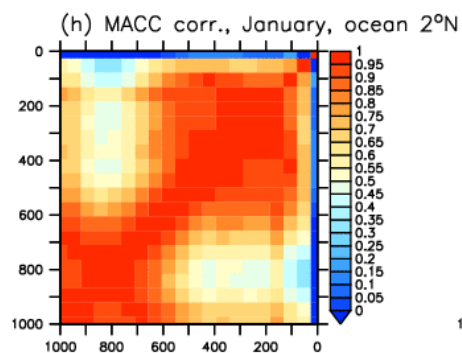
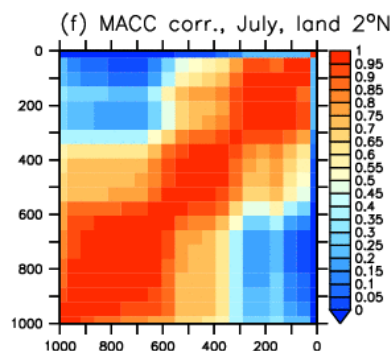
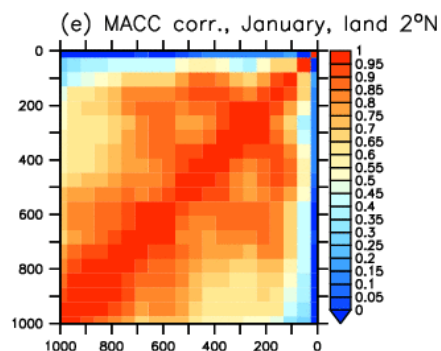


**HBH<sup>T</sup>** in the LSCE inversion system

Both axes are vertical pressures (hPa)

**B** in the ACOS retrievals

Both axes are vertical pressures (hPa)



# Consistent prior error statistics?

## Standard deviations

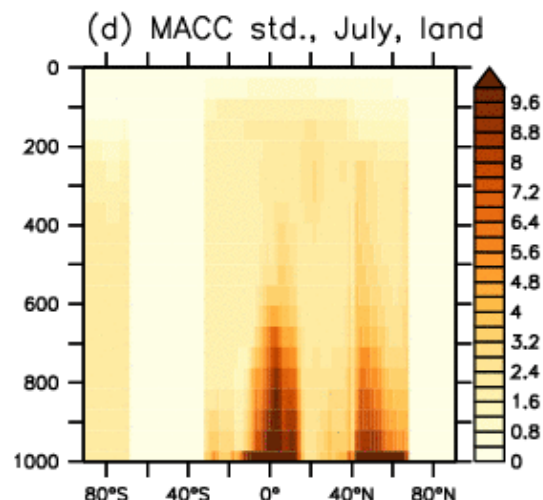
**B** in the ACOS retrievals

$\sigma^{\text{col}} = 12 \text{ ppm}$

The vertical axis shows pressures (hPa)

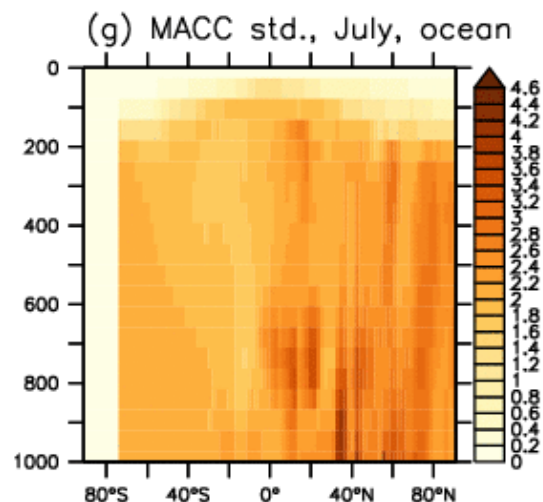
O'Dell et al. (2012)

$\sigma \text{ [ppm]}$   
1.4  
2.5  
3.2  
4.0  
5.6  
6.6  
7.4  
8.2  
9.2  
10.1  
12.2  
14.1  
17.1  
19.9  
24.0  
27.8  
32.7  
37.4  
42.7  
47.7



**HBH<sup>T</sup>** in the LSCE inversion system  
 $\sigma^{\text{col}} \approx 1\text{-}4 \text{ ppm}$

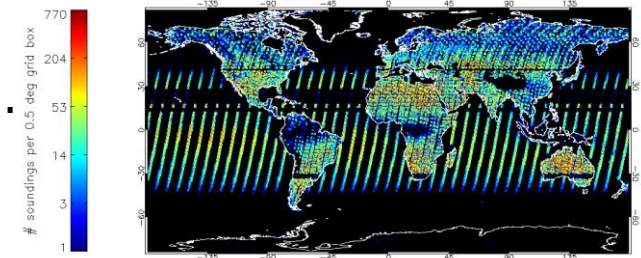
The vertical axis shows pressures (hPa)



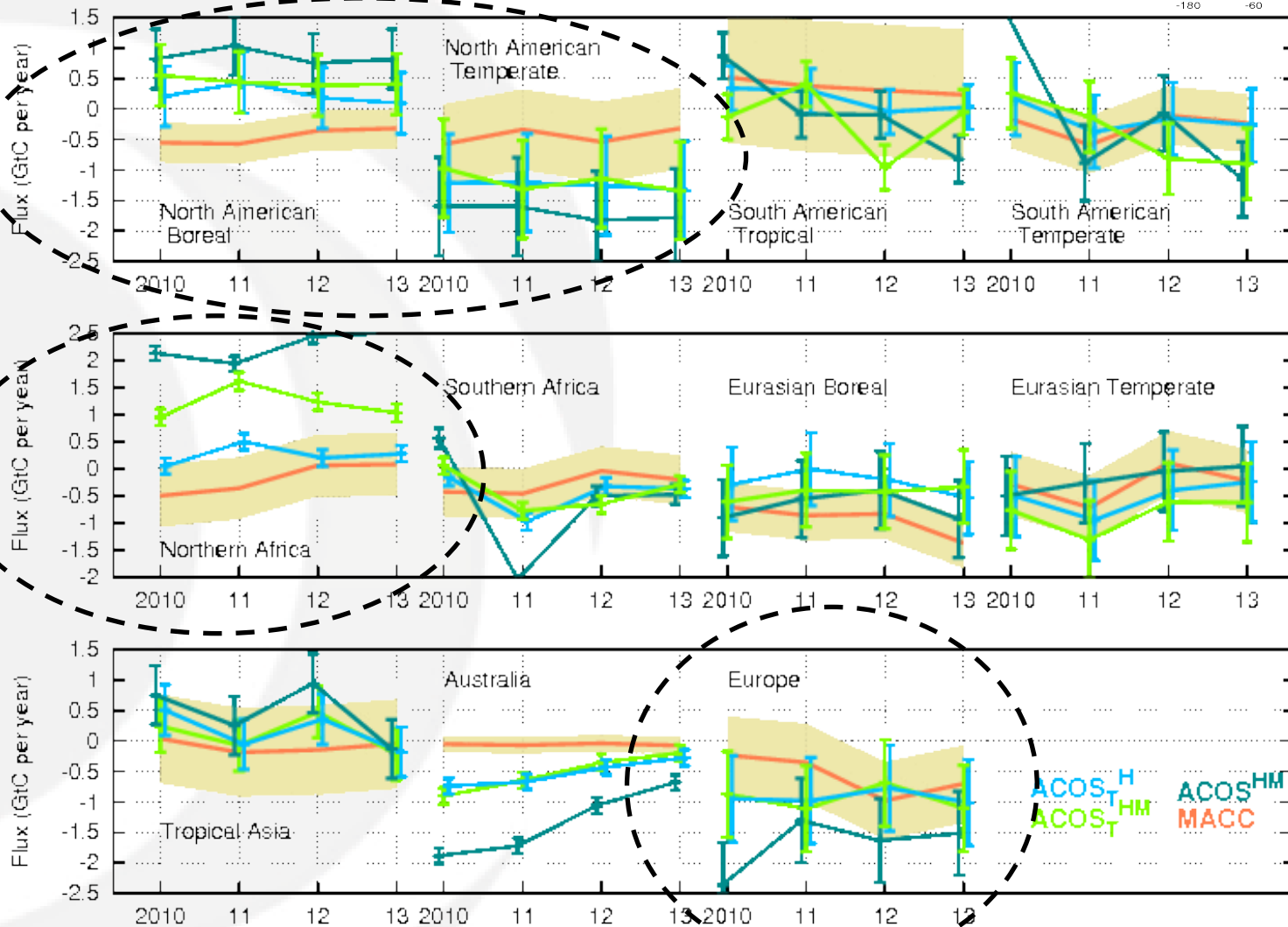
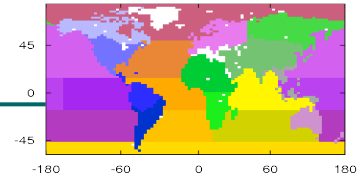


# Changing **B**

- Regenerating the retrievals with a different **B** (collab. with C. O'Dell, CSU).
- ACOS b3.5, high-gain, medium-gain, nadir, glint.
- New **B** (hereafter **B'**) from a frozen climatology of prior error statistics (latitude, month, geotype).
- Ad hoc bias-correction based on MACCv13.1 and using the same parametric formula than ACOS-GOSAT ( $2 \times 5 + 4$  parameters).
- 4 inversions compared over 4 years (2010-2013):
  - MACCv14.2 (surface).
  - ACOS<sup>HM</sup>: Standard b3.5, H-gain and M-gain.
  - ACOS<sub>T</sub><sup>HM</sup>: b3.5 with **B'**, H-gain and M-gain.
  - ACOS<sub>T</sub><sup>H</sup>: b3.5 with **B'**, H-gain only.



# Inverted annual regional budgets over land with $1\sigma$



# Conclusions

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- Satellite-based atmospheric inversions use small  $\text{XCO}_2$  signals, that need to be carefully extracted and characterized.
  - Renews the problem of remotely sensing atmospheric composition.
- Need of better statistical consistency from radiances to fluxes.
  - Official retrievals do not properly account for prior information.
    - Averaging kernels do not peak at the right altitude.
  - Noticeable impact on subcontinental annual budgets (not just random noise).
  - Solutions to tailor existing retrievals to each individual inversion scheme should be offered (through linear algebra) in the same way as averaging kernels are systematically provided.
  - Other smaller issues in the retrievals remain to be solved:
    - Underestimation of atmospheric growth rate,
    - Inclusion of medium-gain data,
    - High latitudes.

# Acknowledgements

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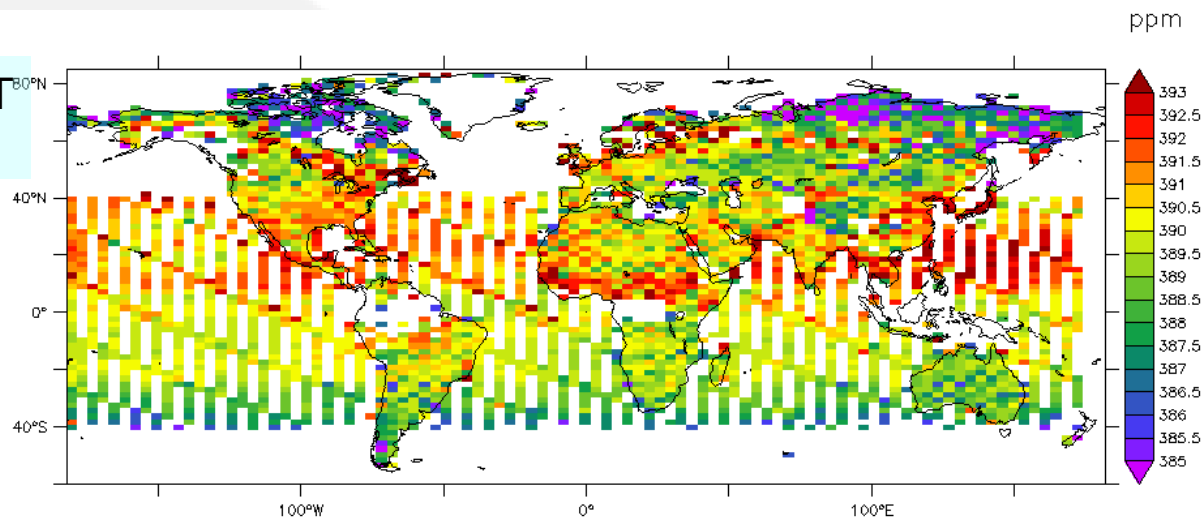
- This work could not have existed without the work of many organisations that have made, archived or distributed surface air sample measurements (e.g., NOAA, WDCGG, RAMCES, ICOS).
- The ACOS GOSAT data can be obtained from <http://co2.jpl.nasa.gov>. They were produced by the ACOS/OCO-2 project at the Jet Propulsion Laboratory, California Institute of Technology, using GOSAT observed spectral radiances made available by the GOSAT project.
- Christopher O'Dell provided critical help to tailor the ACOS-GOSAT retrievals to the LSCE inversion system.

# Back-up slides

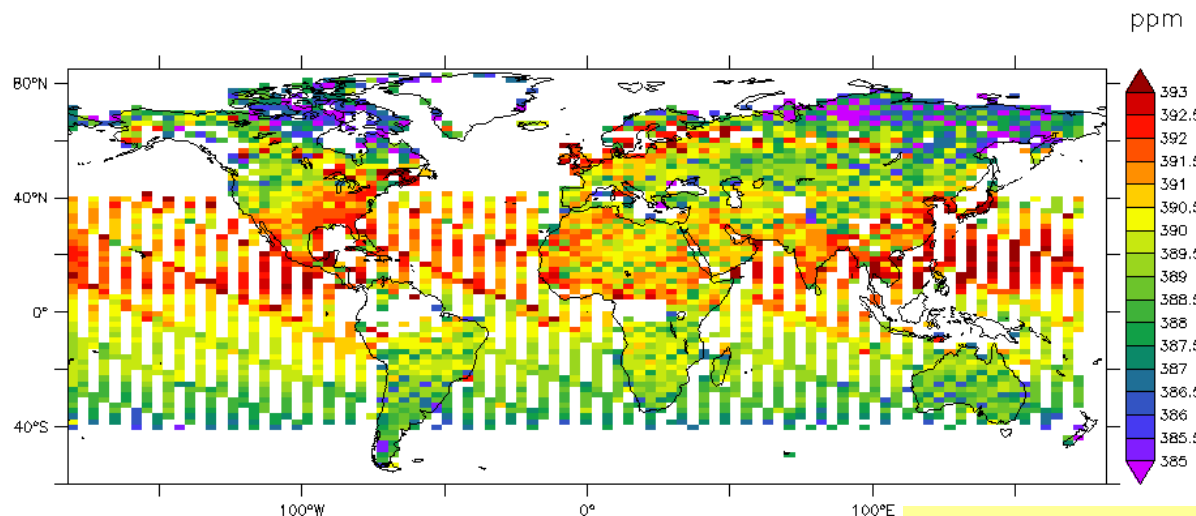
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# XCO<sub>2</sub> 4-yr mean GOSAT and MACC surface inversion

ACOS-GOSAT  
b3.4

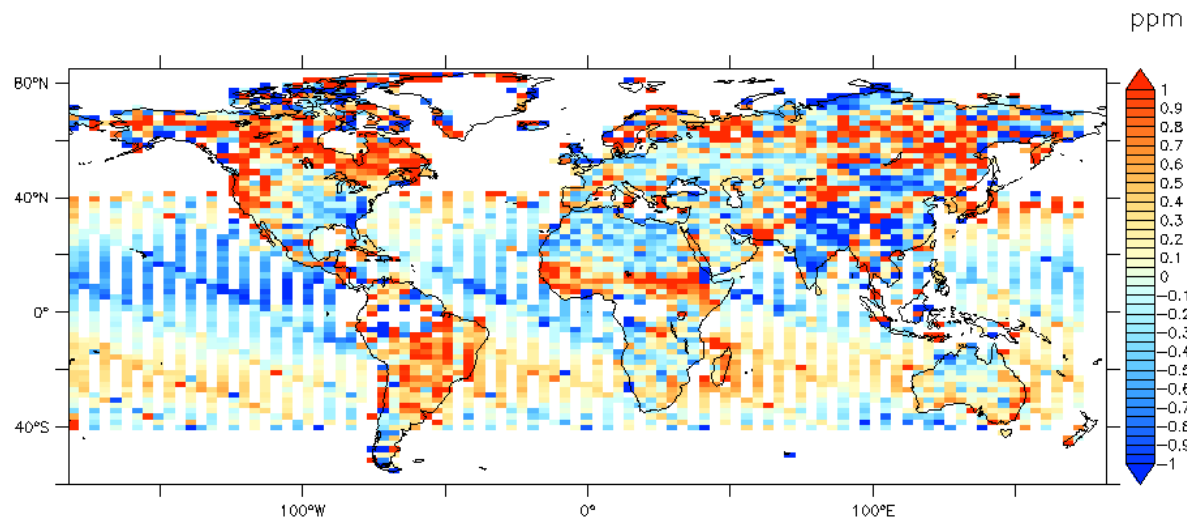


MACC  
v13.1

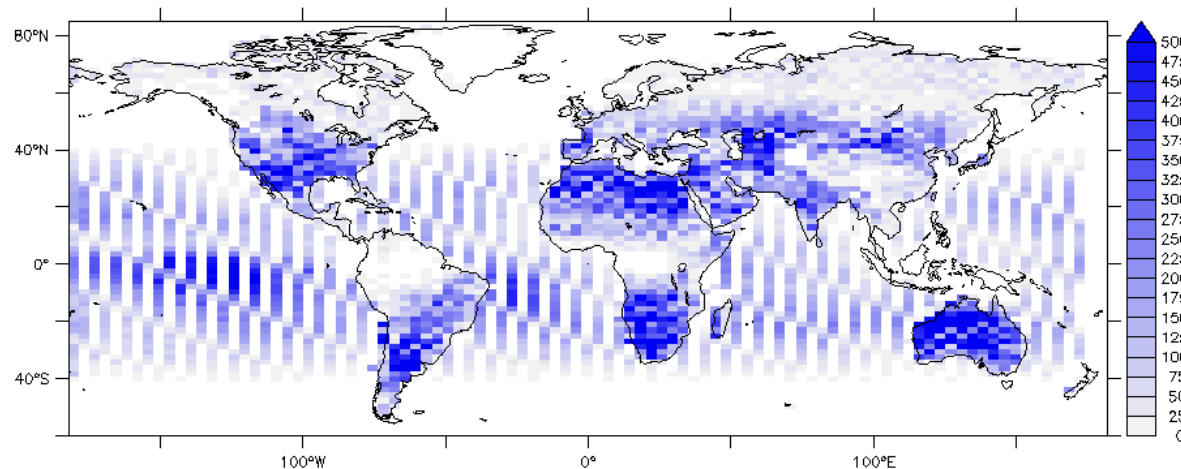


# XCO<sub>2</sub> 4-yr mean GOSAT and MACC surface inversion

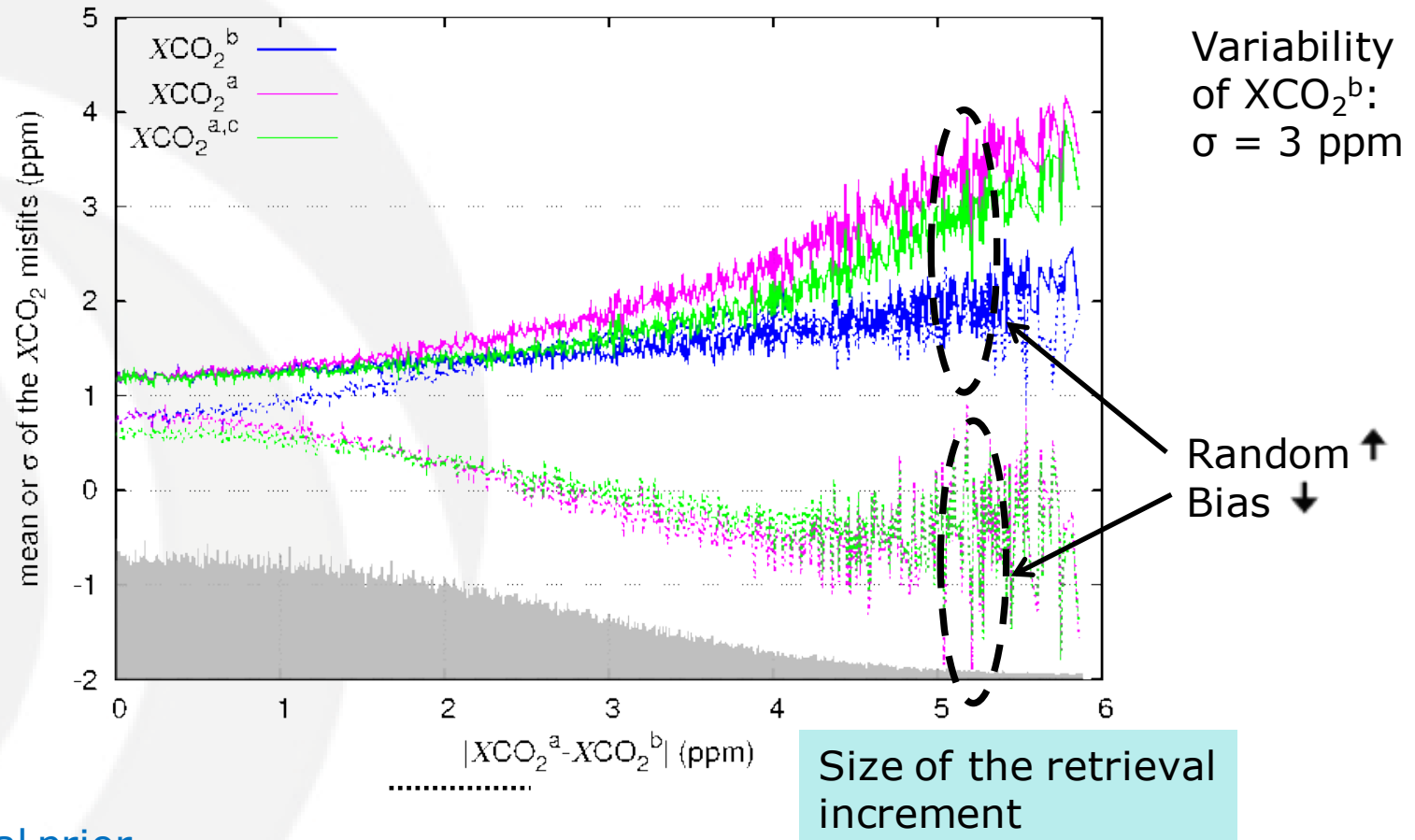
ACOS-GOSAT  
minus MACC



# of data



# Misfits vs. retrieval increment – H gain (land)



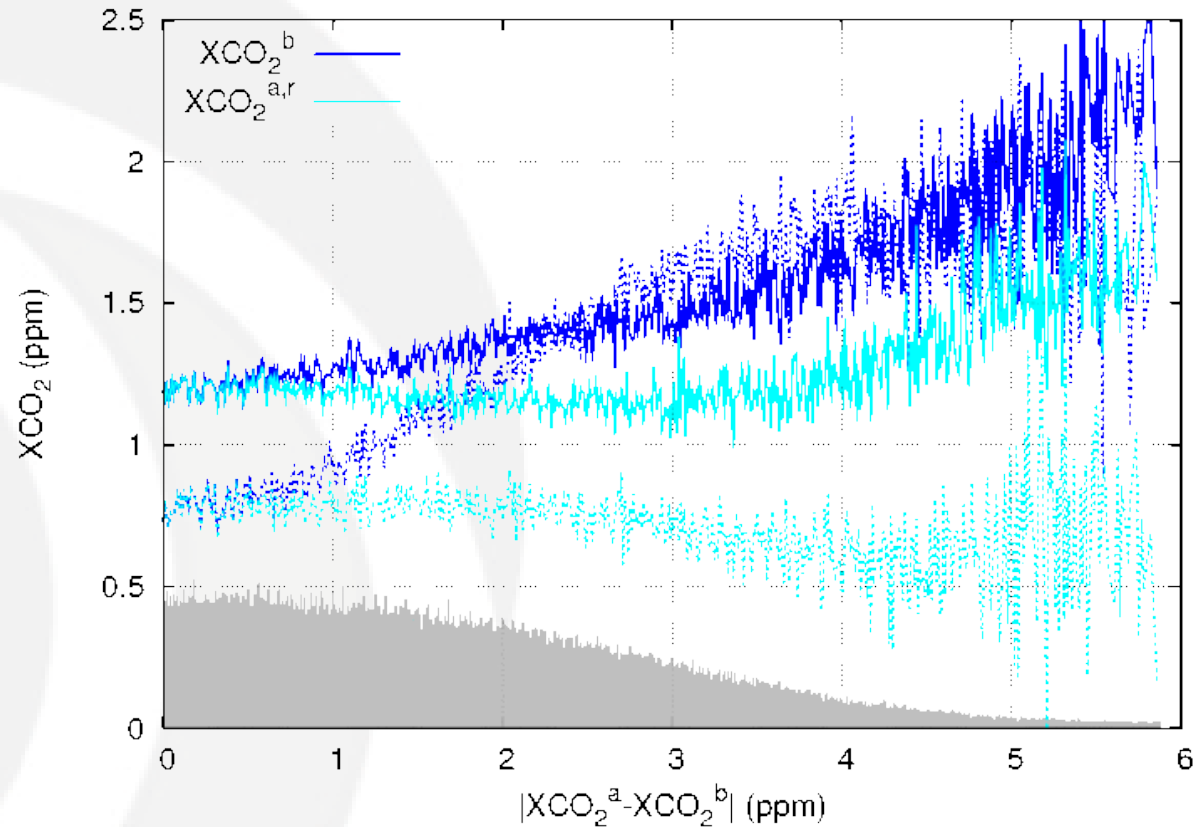
- Misfit bias
- **b**: retrieval prior
- **a**: raw retrieval
- **a,c**: bias-corrected retrieval
- MACC = no AK

MACC vs. TCCON  $\sim 0 \pm 0.9$  ppm

Chevallier (ACPD, 2015)



# Misfits vs. retrieval increment – H gain (land)



- Misfit bias
  - $b$ : retrieval prior
  - $a,r$ : revised retrieval (AK/2), without any bias-correction
  - Unchanged abscissa
  - MACC = no AK
- and std. ....

MACC vs. TCCON  $\sim 0 \pm 0.9$  ppm

Chevallier (ACPD, 2015)